

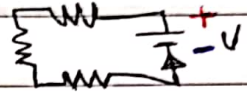
« Introduction »

ch:1

units. A, V, Ω

Ω law:  $\begin{matrix} \nabla \\ V \\ \hline I R \end{matrix}$

Schematic  $\leftrightarrow$  bits



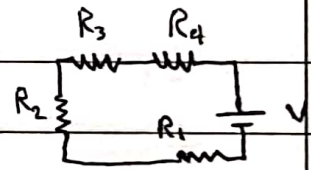
المصادر / مصدر فولتية = فولتية ثابتة وتيار يعتمد على الحمل.  
 مصدر تيار = تيار ثابت وفولتية تعتمد على الحمل.

+ Resistors  
- Source

$P_{dis} = VI$

\* القدرة المستهلكة أو المبددة : تكون موجبة للمقاومات وسالبة للمصدر

سلسلة / Series :  $R_{eq} = R_1 + R_2 + R_3 + R_4$



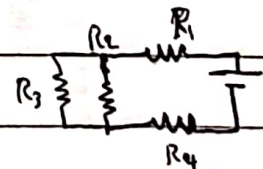
متوازي / Parallel :  $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$



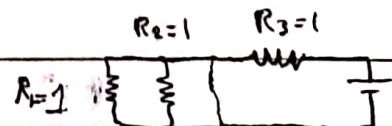
$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$

متوازي  $R_1, R_2$

متنوع / Mixed :



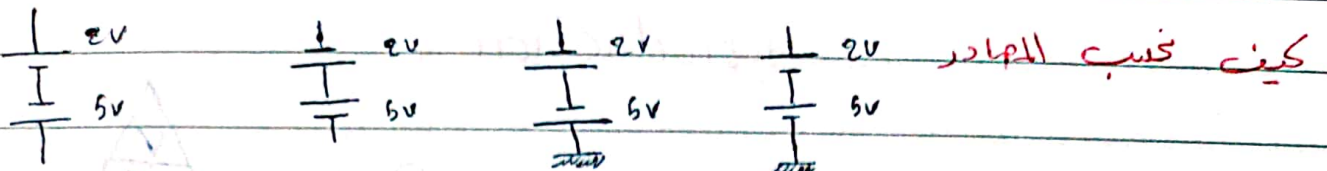
Ex: Find the current?



$R_{eq} = R_3 = 1 \Omega$

$I = \frac{5}{1} = 5 A$

السبب وجود short circuit



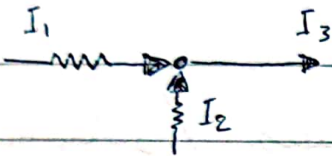
-3

3

-7

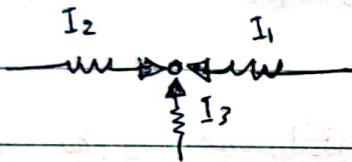
7

عن طريق الاتجاه



$$I_3 = I_1 + I_2 \quad \text{و} \quad I_1 + I_2 + I_3 = 0$$

\* كلما زادت الفولتية زاد التيار والعكس صحيح.



$$I_2 + I_3 + I_1 = 0$$

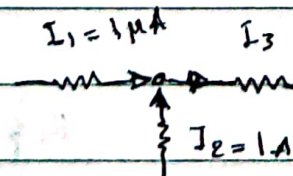
حسب الاتجاه

Ex:

$$I = \frac{V}{R} = \frac{5}{0} = \infty$$



\* السبب Open Circuit

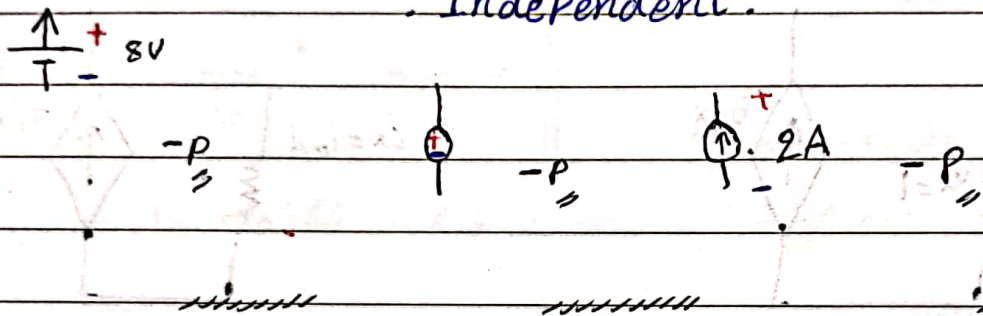


$$I_3 = I_2 = 1A$$

تقريباً لتسهيل الحساب

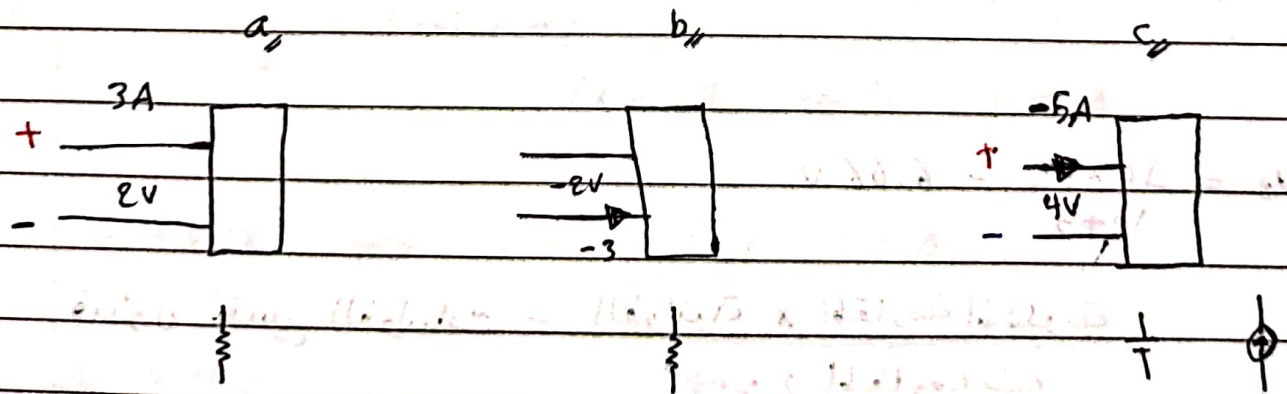
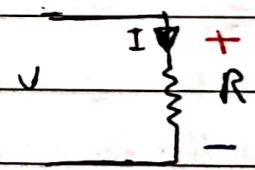
Units :  $\mu A$   
 $mA$   
 $KA$   
 $A$  ,  $V$  ,  $\Omega$  ,  $m$  ,  $s$   
 $mA$   
 $\mu A$   
 $nA$   
 $PA$

Independent.



Power.

$P = IV$



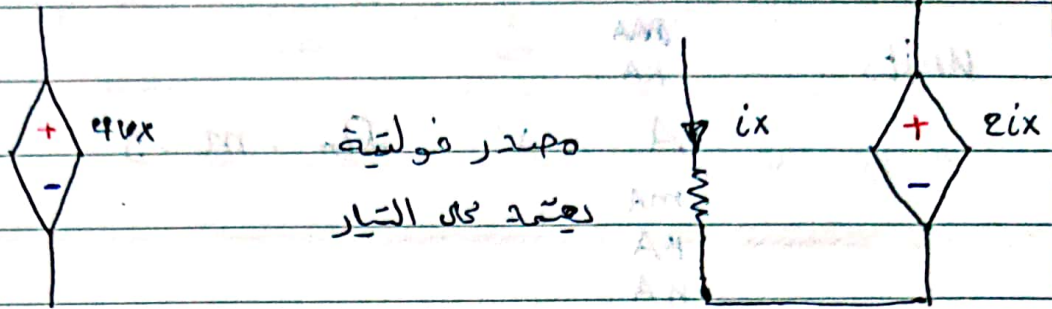
$P = IV$

$= (2) (3) = 6W$   $a$

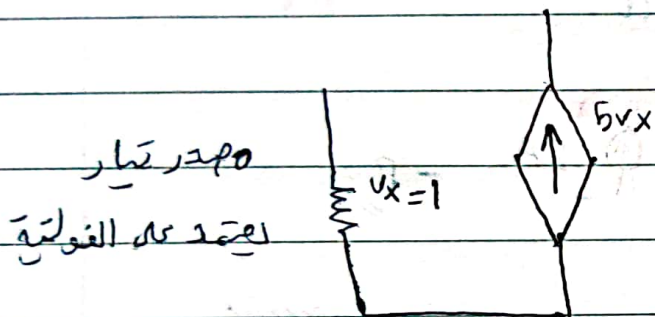
$= (-2) (-3) = 6W$   $b$

$= (-5) (4) = -20W$   $c$

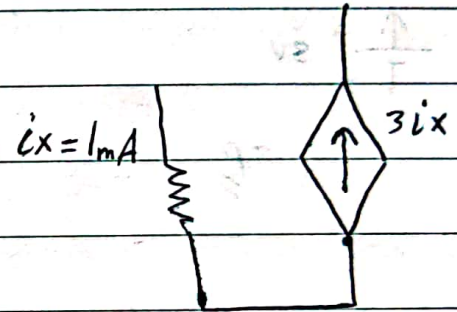
• dependent .



مصدر فولتية  
يعتمد على التيار

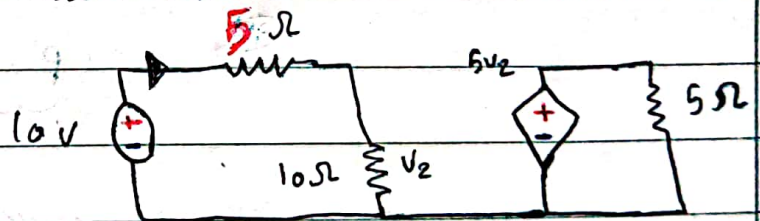


مصدر تيار  
يعتمد على الفولتية



مصدر تيار يعتمد على التيار

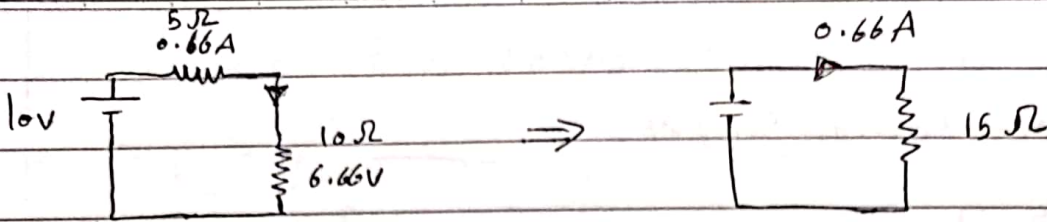
Q/  
find the power of each  
element in fig Below.



$$V_2 = \frac{10 \times 10}{10 + 5} = 6.66 \text{ V}$$

قانون تقسيم الفولتيات = الفولتية × المقاومة المطلوبة  
مجموع المقاومات

Dependent v.s =  $5 \times 6.66 = 33.3 \text{ Volt}$



$$P_{5\Omega} = \frac{V^2}{R} = I^2 R = IV$$

$$= \frac{(3.33)^2}{5} = 2.2 \text{ W}$$

$$P_{10\Omega} = \frac{(6.66)^2}{10} = 4.4 \text{ W}$$

$$P_{10V} = 10 \times 0.66 = 6.6 \text{ W}$$

$$P_{5\Omega} = \frac{(33.3)^2}{5} = 221.7 \text{ W}$$

$$P_{\text{dependent}} = (33.3) \times (6.66) = 221.7 \text{ W}$$

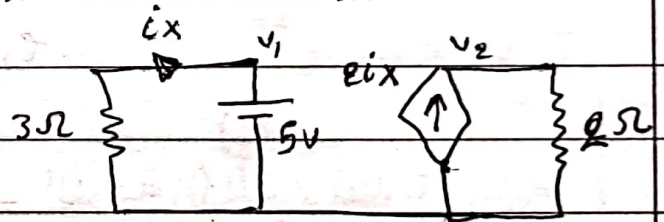
ملاحظة مهمة:

أن المجموع الجبري للقوة

في الدائرة يساوي صفر.

Q/ 1 of 3

find the dependent source current ?



Sol

$$I = \frac{5}{3} = 1.66 \text{ Amp}$$

حساب النتيجة

$$ix = -I \Rightarrow ix = -1.66 \text{ A}$$

$$= +2ix \Rightarrow = +2 \times -1.66 = -3.3 \text{ A}$$

Q/ 2 of 3

find the power

Sol

$$P_{R_1} = \frac{V^2}{R} = \frac{25}{3} = 8.3 \text{ W}$$

$$P_{R_2} = I^2 R = (-3.3)^2 \times 2 = 21 \text{ W}$$

Q/ 3 of 3

Find the power supply

$$P_{5V} = VI = 5 \times (-1.66) = -8 \text{ W}$$

$$P_{eix} = VI = (3.33 \times 2) \times (-3.33) = -22.14$$

ملاحظات:

م / صلاك فرق بين Power supply و بين Power أو Power dissipated

م / المقدر المجهز = القدرة المطبوعه

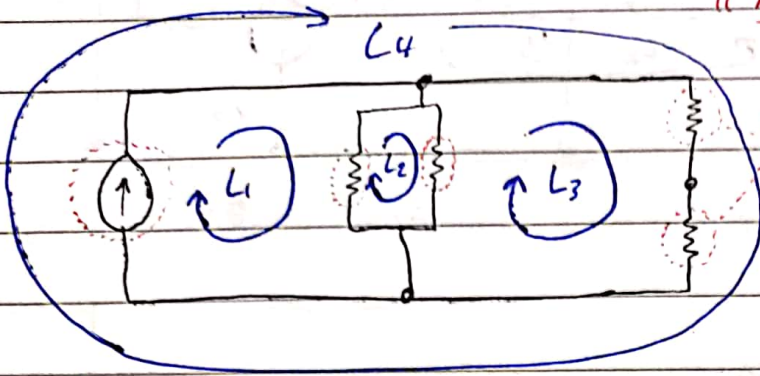
م / قانون تقسيم الفولتيات =  $\frac{\text{الفولتية الكلية} \times \text{المقاومة المصنعة}}{\text{مجموع المقاومات}}$

م / قانون تقسيم التيارات =  $\frac{\text{التيار الكلي} \times \text{المقاومة البعيدة}}{\text{مجموع المقاومات}}$

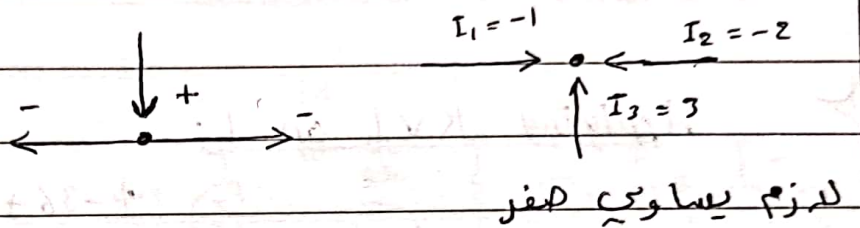
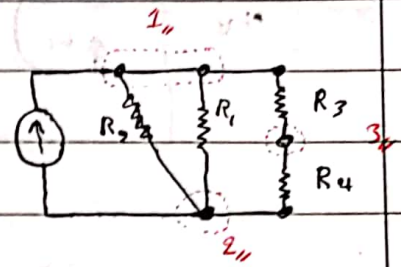
# Node Path Loops Branches

« K.C.L. »

ch: 3



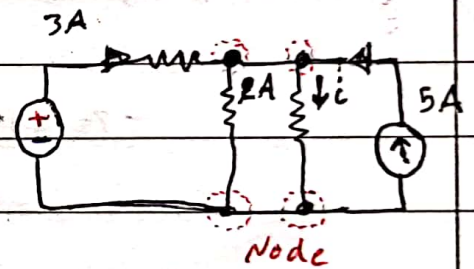
Branches



\* التيارات الداخلة تساوي التيارات الخارجة

@

find the current I?



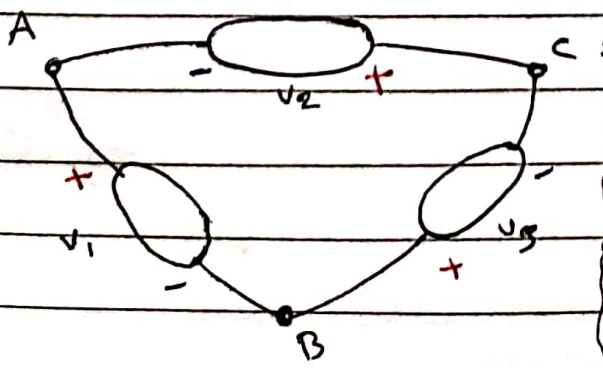
sol

$$(3) + (-2) + (-i) + 5 = 0$$

$$i = 6 \text{ Amp.}$$

« K.V.L. »

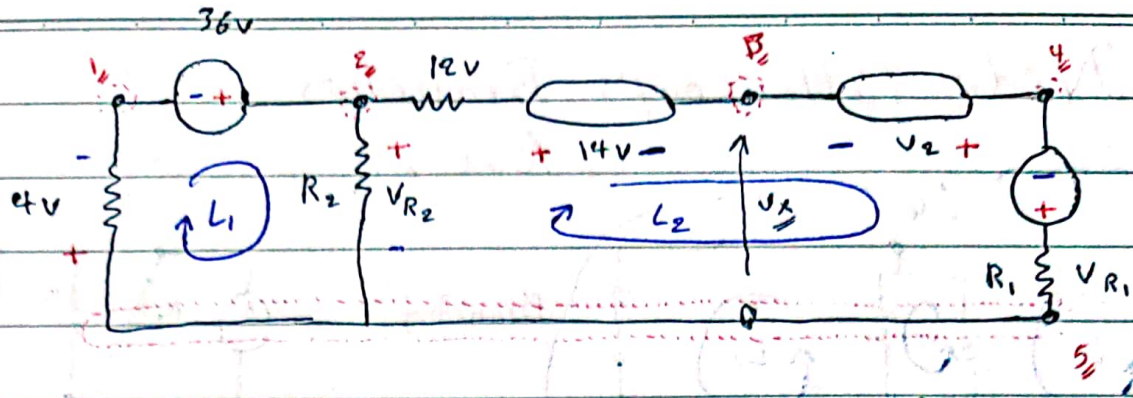
المجموع الجبري للفولتيات في أي لوب يساوي صفر



$$V_1 + V_2 + V_3 = 0$$

$$-V_1 - V_2 - V_3 = 0 \quad (\neq -1)$$

$$V_1 + V_2 + V_3 = 0$$



Q/

find  $V_{R_2}$  and find  $V_x$ 

sol/

Applying KVL on  $L_1$ 

$$4 - 36 + V_{R_2} = 0 \quad V_{R_2} = 32 \text{ volt}$$

sol/

Applying KVL on  $L_2$ 

$$-32 + 12 + 14 + V_x = 0 \quad V_x = 6 \text{ volt}$$

\* إذا حسبنا بالعكس أيضاً نصل إلى نفس الناتج

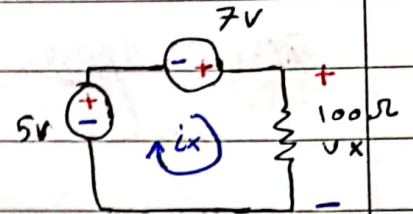
\* KCL يطبق على النقاط فقط أي على node

\* KVL يطبق على اللوops فقط أي على loop



Q

find the current  $i_x$



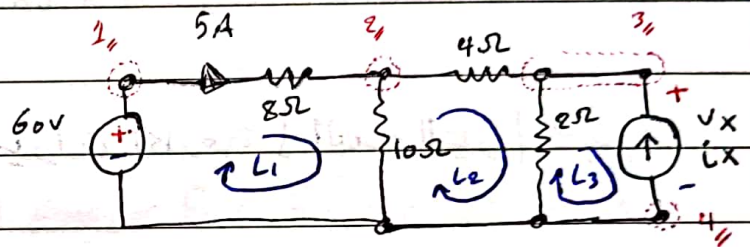
Sol

$$-5 - 7 + V_x = 0 \quad , \quad V_x = 12$$

$$i_x = \frac{V_x}{R} = \frac{12}{100} = 0.12A$$

Q

find  $V_x$  and  $i_x$



Sol

Applying K.V.L on  $L_1$

first find  $V_{R8}$  /  $V_{R8} = 5 \times 8 = 40V$

Now Applying K.V.L on  $L_2$

$$-60 + 40 + V_{R10} = 0 \quad \boxed{V_{R10} = 20 \text{ volt}}$$

Find  $I_{R10}$

$$I_{R10} = \frac{20}{10} = 2A$$

Now Applying KCL at node

$$5 - 2 - I_{R4} = 0$$

$$I_{R4} = 3A$$

Find  $V_{R4}$

$$V_{R4} = IR = 3 \times 4 = 12 \text{ volt}$$

Now Applying K.V.L on  $L_2$

$$-20 + 12 + V_{R_2} = 0$$

$$V_{R_2} = 8V = V_x$$

find  $I_{R_2} = \frac{V_{R_2}}{R_2} = \frac{8}{2} \quad I_{R_2} = 4A$

Now Applying K.C.L at  $n_3$

$$3 - 4 + i_x = 0 \Rightarrow i_x = 1A$$

\* للتأكد من اكل نحسب التيارات الخارجة [بالنسبة للتيار] يجب أن تساوي صفر والقولية كذلك نطبقها على الدائرة كاملة أيضاً يجب أن تساوي صفر

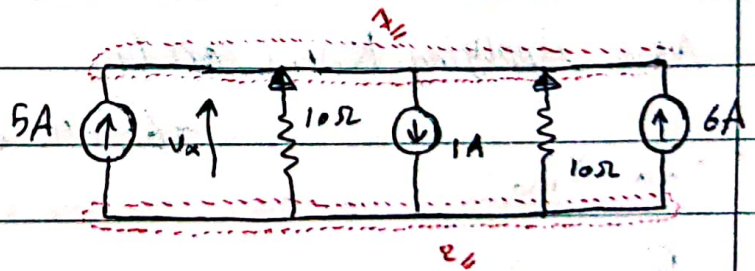
Applying KCL at  $n_4$

$$-5 + 2 + 4 - 1 = 0$$

Applying KVL out

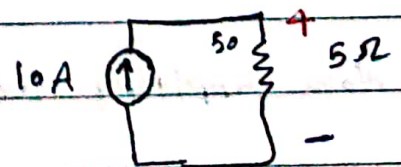
$$-60 + 40 + 12 + 8 = 0$$

Q/ find  $V_x$



Sol

With Best wishes.

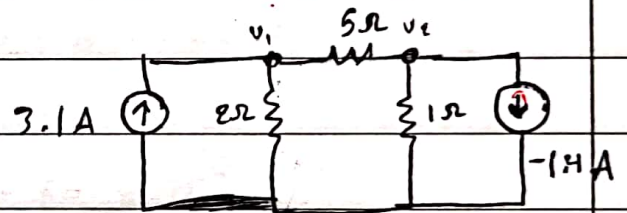


Kirchhoff's Voltage Law.  
Kirchhoff's Current Law.

# ✿ Nodal Analysis ✿

1. Determin the nodes. ١ - حدد العقد
2. Choose 1 node as Reference. ٢ - اختر أحد العقد كمرجع
3. Apply kcl at each node. ٣ - تطبق kcl على كل عقدة.
4. Solve the equations ٤ - حل المعادلات

Q find the dissipated power for the circuit below



Sol Applying kcl at  $v_1$

$$3.1 - \frac{v_1}{2} - \left(\frac{v_1 - v_2}{5}\right) = 0 \quad \text{--- (1)}$$

Applying kcl  $v_2$

$$\frac{v_1 - v_2}{5} - \frac{v_2}{1} - (-1.4) = 0 \quad \text{--- (2)}$$

Now multiply (1)  $\times 10$

$$31 - 5v_1 - 2v_1 + 2v_2 = 0$$

$$31 - 7v_1 + 2v_2 = 0 \quad \text{--- (3)}$$

Now multiply (2)  $\times 5$

$$v_1 - v_2 - 5v_2 + 7 = 0$$

$$v_1 - 6v_2 + 7 = 0 \quad \text{--- (4)}$$

Now ③  $\times 3$  + ④

$$93 - 21V_1 + 6V_2 = 0$$

$$V_1 - 6V_2 + 7 = 0$$

$$-20V_1 + 100 = 0$$

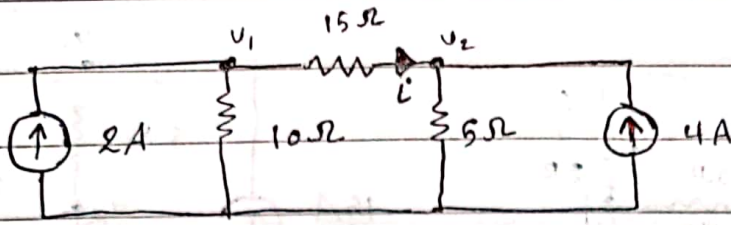
$$\Rightarrow V_1 = 5$$

لصوفى بي ④

$$5 - 6V_2 + 7 = 0$$

$$V_2 = 2$$

~~0~~



find  $i$

Sol

Applying KCL at  $v_1$

$$2 - \frac{v_1}{10} - \left( \frac{v_1 - v_2}{15} \right) = 0 \quad \dots (1)$$

Applying KCL at  $v_2$

$$\frac{v_1 - v_2}{15} - \frac{v_2}{5} + 4 = 0 \quad \dots (2)$$

Multiply (1) \* 30

$$60 - 3v_1 - 2v_1 + 2v_2 = 0$$

$$60 - 5v_1 + 2v_2 = 0 \quad \dots (3)$$

Multiply (2) \* 15

$$v_1 - v_2 - 3v_2 + 60 = 0$$

$$v_1 - 4v_2 + 60 = 0 \quad \dots (4)$$

Multiply (3) \* 2

and plus with (4)

$$120 - 10v_1 + 4v_2 = 0$$

$$60 + v_1 - 4v_2 = 0$$

$$180 - 9v_2 = 0$$

$$v_1 = 20 \text{ V}$$

نصفها  
(4)  $\frac{1}{2}$

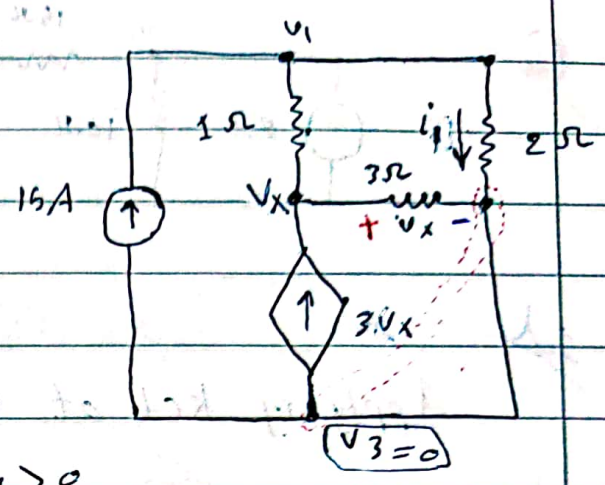
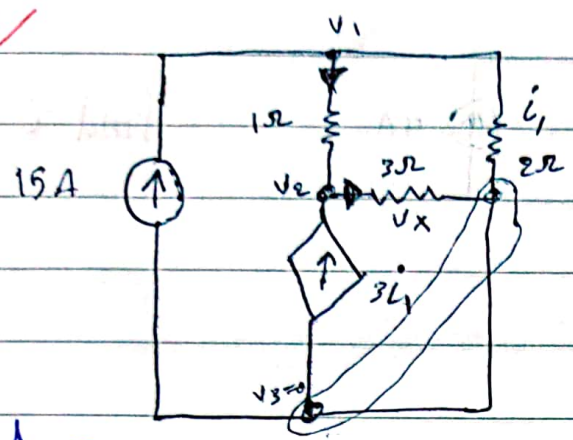
$$20 - 4v_2 + 60 = 0$$

$$v_2 = 20 \text{ V}$$

$$i = \frac{20 - 20}{15} = 0$$

# Find the diss power of $R_{3\Omega}$

Q



Scanned

$$V_1 > V_2 \quad V_1 > 0 \quad V_2 > 0$$

$$15 - \frac{(V_1 - V_2)}{1} - \frac{V_1}{2} = 0 \quad \dots \textcircled{1}$$

at  $V_2$   $\therefore V_2 > 0$

$$-\left(\frac{V_2 - V_1}{1}\right) - \frac{V_2}{3} + 3i_1 = 0 \quad \dots \textcircled{2}$$

$$i_1 = \frac{V_1}{2} \quad \dots \textcircled{3} \quad \text{نقطة في 2}$$

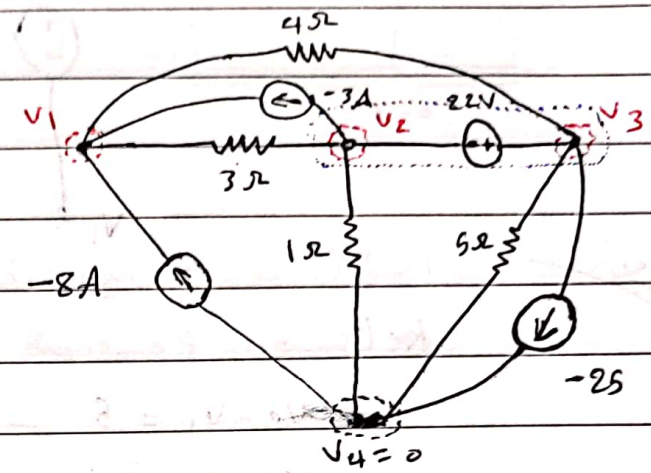
$$-\left(\frac{V_2 - V_1}{1}\right) - \frac{V_2}{3} + \frac{3V_1}{2} = 0$$

\* تطبيق KCL <sup>at node 1</sup> تربط في كل الاتجاهات خارجا

\* All current is out of the node.

Ex: What is the current through the voltage supply.

Sol



KCL  $v_1$

$$-8 - 3 - \frac{(v_1 - v_2)}{3} - \frac{(v_1 - v_3)}{4} = 0 \quad \text{--- (1)}$$

KCL  $v_2$

$$-\frac{(v_2 - v_1)}{3} + 3 - \frac{v_2}{1} = 0 \quad \text{--- (2)}$$

\* لا يمكن حساب التيار في نود كالمعتاد، فولتية

\* أي نودين أو أكثر مرتبطين بهما فولتية يعتبرون نود واحد

ويسمى **Super node**

KCL at Super Node:

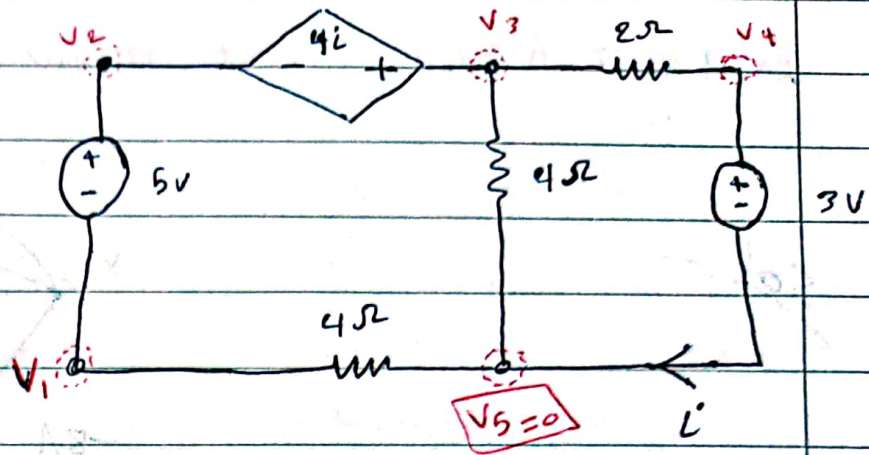
$(v_2, v_3)$  Super Node

$$-(-3) - \frac{(v_2 - v_1)}{3} - \frac{v_2}{1} - \frac{v_3}{5} - (-25) - \frac{(v_3 - v_1)}{4} = 0 \quad \text{--- (3)}$$

$$v_3 - v_2 = 22V \quad \text{--- (3)}$$

to find the current I  $v_2$  نستغل في

find the current  $i$



Sol  
kcl

$$V_2 - V_1 = 5 \quad \text{--- (1)}$$

$$V_3 - V_2 = 4i \quad \text{--- (2)}$$

$$V_4 = 3 \quad \text{--- (3)}$$

Applying kcl at  $V_2, V_3, V_1$

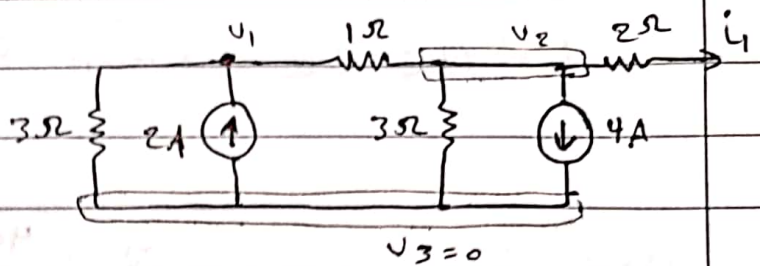
super node

$$-\frac{(V_3 - V_4)}{2} - \frac{V_3}{4} - \frac{V_1}{4} = 0 \quad \text{--- (4)}$$

$$i = \frac{V_3 - V_4}{2} \quad \text{--- (5)}$$



Q/ quiz A



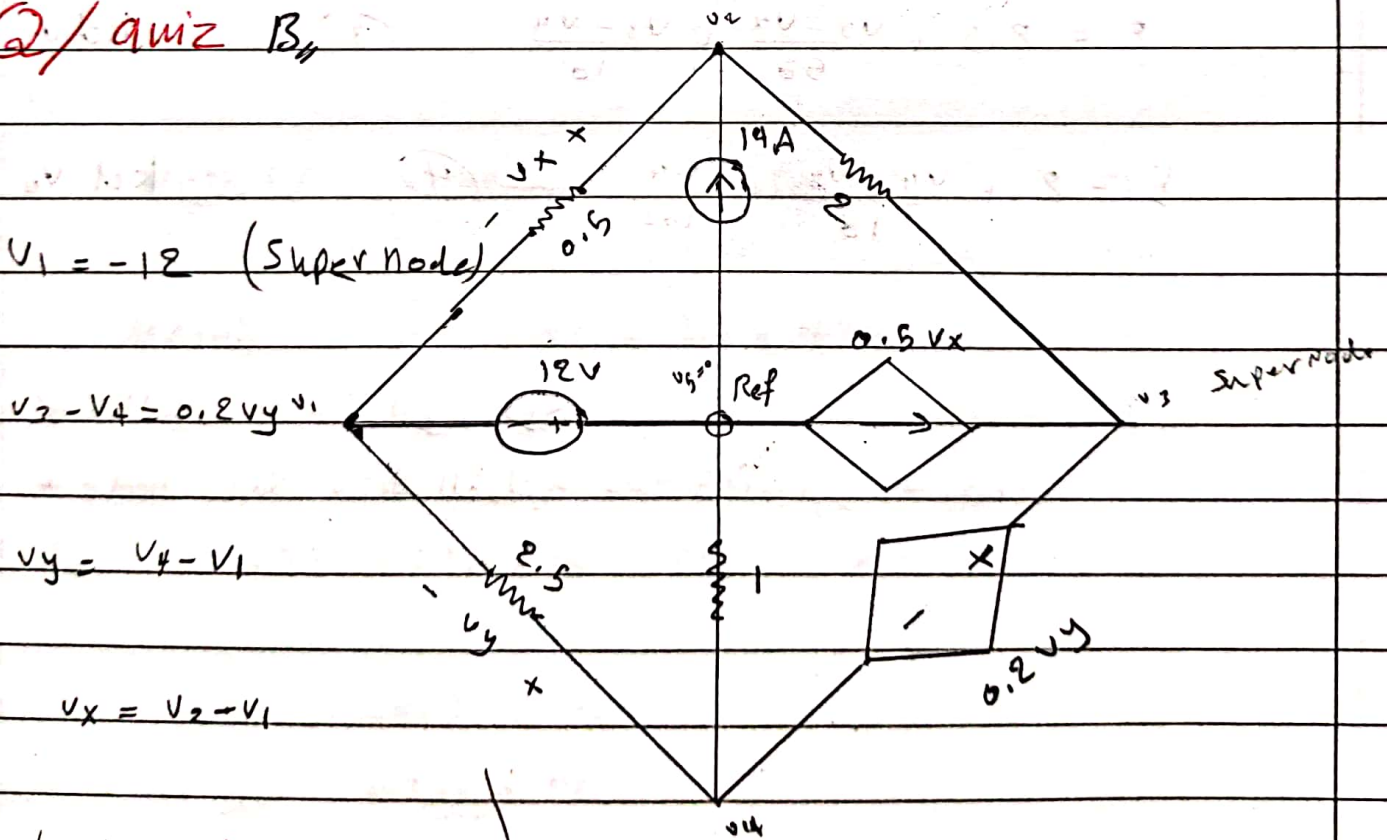
Sol

\* طبقاً لسؤال كان مقاومتي ١Ω و ٢Ω هما المتوالي  
ولكن جهتيهم وهما نحو مقاومة ومدى ٣Ω

$$-\frac{v_1}{3} + 2 - (v_1 - v_2) = 0 \quad \text{--- (1)}$$

$$-\frac{(v_2 - v_1)}{1} - \frac{v_2}{3} - 4 = 0 \quad \text{--- (2)}$$

Q/ quiz B



$$v_1 = -12 \text{ (SuperNode)}$$

$$v_2 - v_4 = 0.2v_y$$

$$v_y = v_4 - v_1$$

$$v_x = v_2 - v_1$$

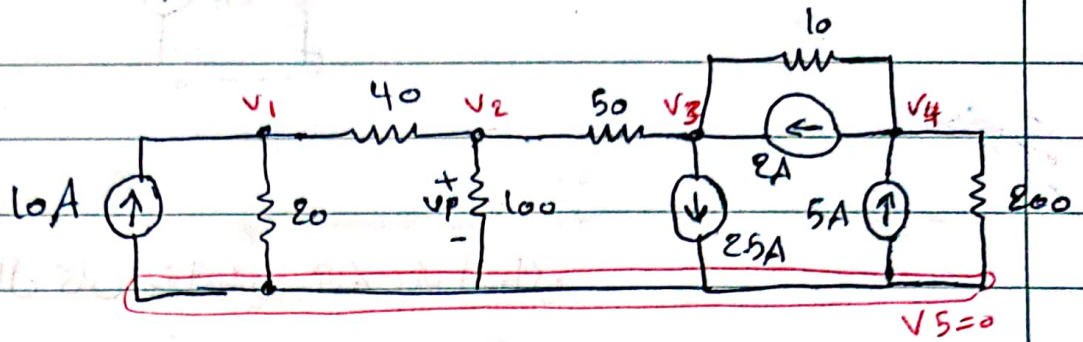
KCL at v2

$$\frac{v_1 - v_1}{0.5} + \frac{v_2 - v_3}{2} = 14$$

$$0.5v_x - 2 - 1 - 2.5v_y$$

v3 SuperNode

Q/ for the circuit shown find  $v_p$



Sol

① تحديد النودات

$$10 = \frac{v_1 - v_2}{40} + \frac{v_1}{20} \quad \text{--- (1)}$$

kcl  $v_1$  (2)

kcl  $v_2$

$$0 = -\left(\frac{v_2 - v_3}{50}\right) - \frac{v_2}{100} - \frac{v_2 - v_1}{40} \quad \text{--- (2)}$$

$$2 = 2.5 + \frac{v_3 - v_2}{50} + \frac{v_3 - v_4}{10} \quad \text{--- (3)}$$

kcl  $v_3$

$$5 = 2 + \frac{v_4 - v_3}{10} + \frac{v_4}{100} \quad \text{--- (4)}$$

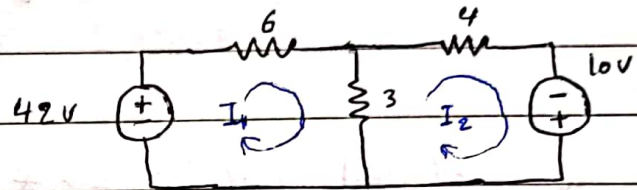
kcl  $v_4$

\* التيار لا يجوز لسوبر نود.  
\* Super node فقط للفوياته يعتمد او غير يعتمد.

# ♥ MESH Analysis ♥

Mesh: هو لوب واحد دونه تداخل أي الرسم يكون مسطح  
دونه تقاطع الخطوط.

Ex:



1- Simplify

2- Mesh حدد

3- I

4- Applying KVL at Mesh.

Sol

$$\text{Mesh 1/} \quad -42 + 6I_1 + 3(I_1 - I_2) = 0 \quad \text{--- (1)}$$

$$\text{Mesh 2/} \quad -10 + 3(I_2 - I_1) + 4I_2 = 0 \quad \text{--- (2)}$$

$$9I_1 - 3I_2 = 42 \quad \text{--- (3)}$$

$$-3I_1 + 7I_2 = 10 \quad \text{--- (4) } \times 3$$

$$-9I_1 + 21I_2 = 30$$

$$+ \quad 9I_1 - 3I_2 = 42$$

$$0 + 18I_2 = 72 \Rightarrow I_2 = 4$$

$$9I_1 - 3(4) = 42 \Rightarrow 9I_1 = 42 + 12 = 54$$

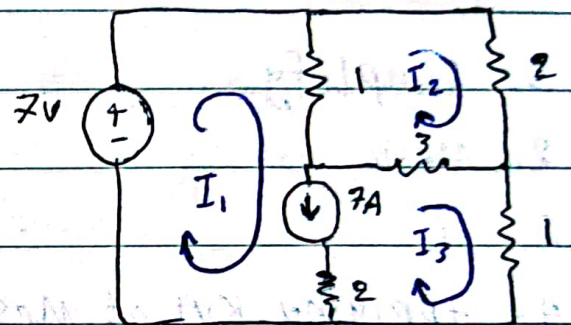
$$I_1 = 6$$

Super node

Make في المثال السابق إذا نتج تطبيق KCL فإن هناك للمصدرين وبالتالي لتبقي نقطة واحدة كالمسألة.

Exs find the Power Supply by 7V

\* مصدر التيار لا يمكن ايجاد الفولتية له



Sol

1- mesh 2

$$2I_2 + 3(I_2 - I_3) + 1(I_2 - I_1) = 0 \quad \text{--- (1)}$$

2- mesh 1, 3 (Super mesh)

$$-7 + 1(I_1 - I_2) + 3(I_3 - I_2) + 1 \times I_3 = 0 \quad \text{--- (2)}$$

$$I_1 - I_3 = 7 \quad \text{--- (3)}$$

$$2I_2 + 3I_2 - 3I_3 + I_2 - I_1 = 0$$

$$-I_1 + 6I_2 - 3I_3 = 0 \quad \text{--- (4)}$$

$$-7 + I_1 - I_2 + 3I_3 - 3I_2 + I_3 = 0$$

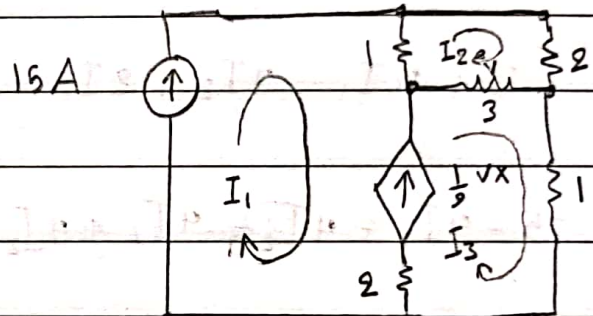
$$I_1 - 4I_2 + 4I_3 = 7 \quad \text{--- (5)}$$

$$I_1 - I_3 = 7 \quad \text{--- (6)}$$

$$-I_1 + 6I_2 - 3I_3 = 0 \quad \text{--- (4)}$$

Ex: find the current of all mesh

- 1- simplify
- 2- Mesh
- 3- Super mesh



KVL at  $I_2$

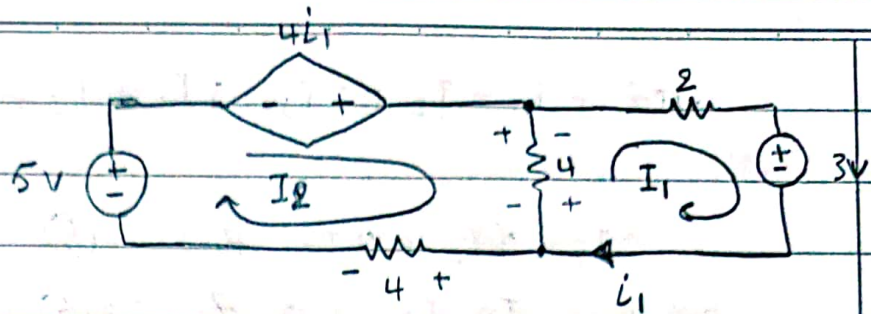
$$2I_2 + 3(I_2 - I_3) - 1(I_2 - I_1) = 0 \quad \text{--- (6)}$$

$$I_1 = 15 \quad \text{--- (2)}$$

$$I_3 - I_1 = \frac{1}{9} V_x \quad \text{--- (3)}$$

$$V = (I_3 - I_2) 3 \quad \text{--- (4)}$$

$I_3, I_1$  Super Mesh حل 5 جوز 11 \*

Ex: find  $I_1, I_2$ KVL at  $I_1$ 

$$3 + 4(I_2 - I_1) + 2I_1 = 0 \quad \text{--- (1)}$$

KVL at  $I_2$ 

$$-5 - 4I_1 + 4(I_2 - I_1) + 4I_2 = 0 \quad \text{--- (2)}$$

$$3 + 4I_1 - 4I_2 + 2I_1 = 0 \Rightarrow 6I_1 + 3 - 4I_2 = 0 \quad \text{--- (3)}$$

(A2)

$$-5 - 4I_1 + 4I_2 - 4I_1 + 4I_2 = 0 \Rightarrow -8I_1 + 8I_2 - 5 = 0 \quad \text{--- (4)}$$

$$12I_1 + 6 - 8I_2 = 0$$

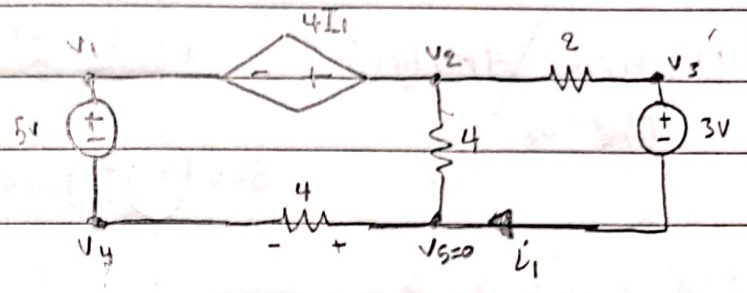
$$\underline{-8I_1 + 8I_2 - 5 = 0}$$

$$4I_1 + 1 = 0 \Rightarrow I_1 = \frac{-1}{4} = -250 \text{ mA}$$

$$I_2 = 375 \text{ mA}$$

Ex: find  $I_1$  by using Nodal Analysis

- 1 - Simplify
- 2 - Node  $\rightarrow$   $\infty$



$V_1, V_3, V_4$  {Super Node}

Applying Kcl at  $V_2$

$$\frac{-V_4}{4} + \frac{V_2}{4} + \frac{V_2 - V_3}{2} = 0 \quad (1)$$

$$V_1 - V_4 = 5 \quad (2)$$

$$V_2 - V_1 = 4I_1 \quad (3)$$

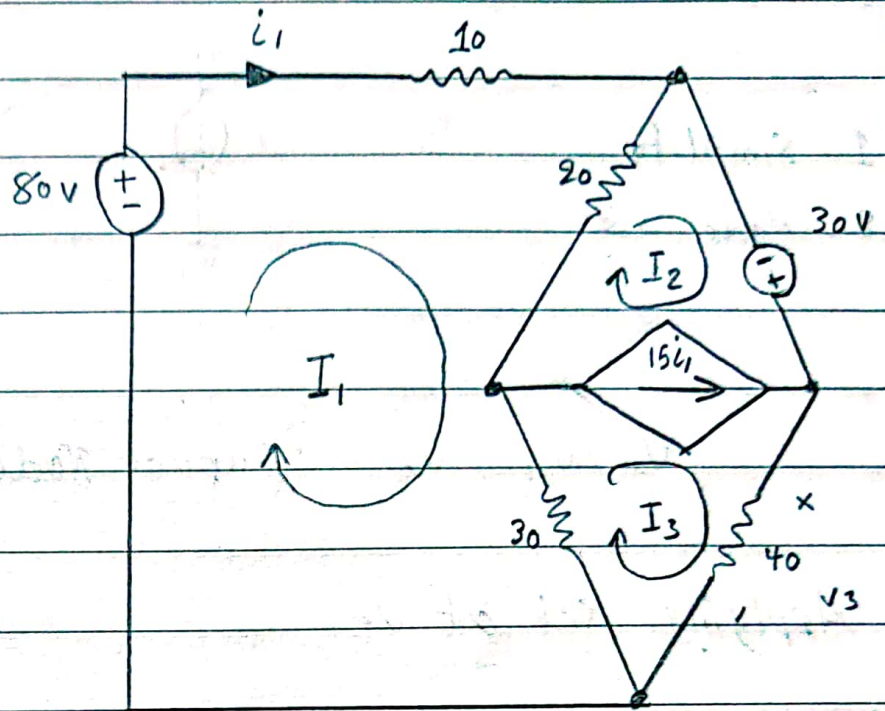
$$V_3 = 3 \quad (4)$$

$$I_1 = \frac{(V_2 - V_3)}{2} \quad (5)$$

Ex: Find  $i_1$  using 1) Mesh Analysis 2) Nodal Analysis

1) Mesh Analysis

Find  $v_3$



KVL at  $I_1$

$$-80 + 10I_1 + 20(I_1 - I_2) + 30(I_1 - I_3) = 0 \quad \text{--- (1)}$$

KVL at  $I_2, I_3$  {Super Mesh}

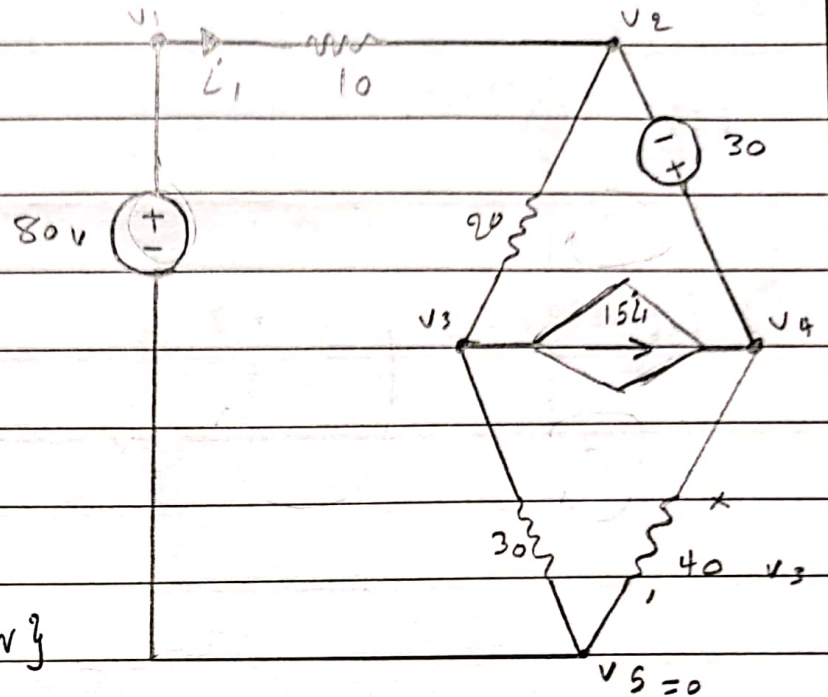
$$-30 + 40I_3 + 30(I_3 - I_1) + 20(I_2 - I_1) = 0 \quad \text{--- (2)}$$

$$I_3 - I_2 = 15I_1$$



Ex: find  $v_3$  in using nodal analysis

Sol



$$v_1 = 80 \quad \text{--- (1)}$$

$$v_4 - v_2 = 30 \quad \text{--- (2)}$$

Kcl at  $v_2, v_4$  {S.N}

$$-\frac{(v_2 - v_1)}{10} - \frac{(v_2 - v_3)}{20} + 15i_1 - \frac{v_4}{40} = 0 \quad \text{--- (3)}$$

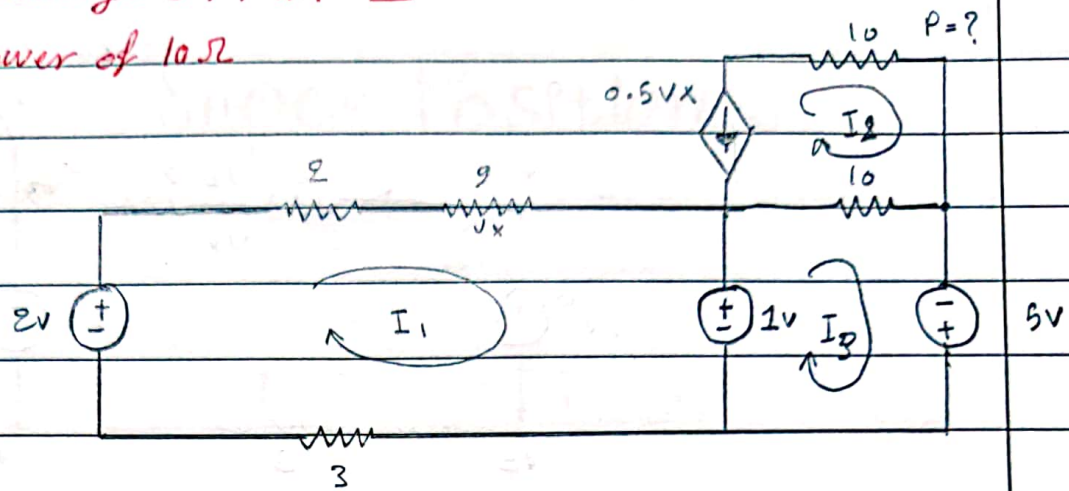
Kcl at  $v_3$

$$-15i_1 - \frac{(v_3 - v_2)}{20} - \frac{v_3}{30} = 0 \quad \text{--- (4)}$$

$$i_1 = \frac{v_1 - v_2}{10} \quad \text{--- (5)}$$

Using Mesh Analysis, find  $v_x$   
 or: find the power of  $10\Omega$

شكل 4,65



Sol

1- ✓

2- Determine Mesh

$$I_2 = -0.5v_x \quad \text{--- (1)}$$

KVL at  $I_1$ 

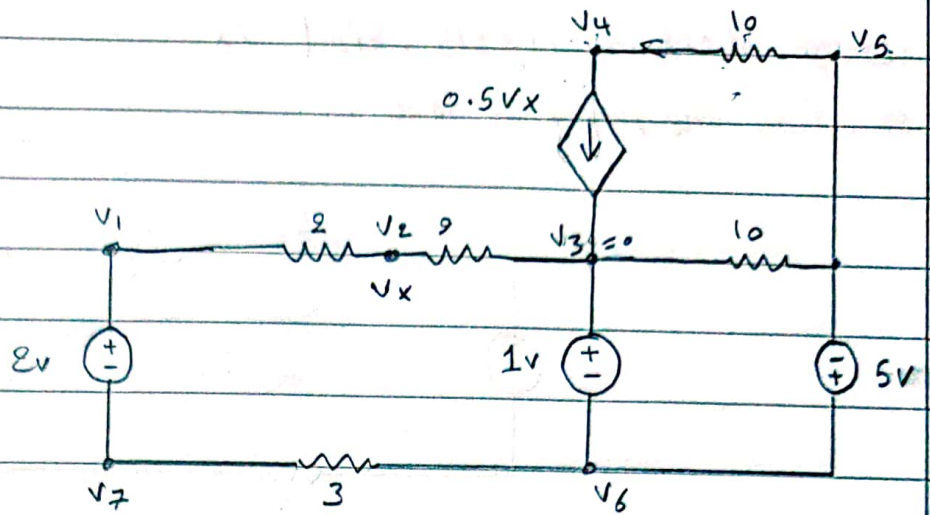
$$-2 + 2I_1 + 9I_1 + 1 + 3I_1 = 0 \quad \text{--- (2)}$$

KVL at  $I_3$ 

$$-1 + (I_3 + I_2)10 - 5 = 0 \quad \text{--- (3)}$$

$$v_x = I_1 \times 9 \quad \text{--- (4)}$$

\* Re solve using Nodal Analysis



Sol

$$V_1 - V_7 = 2 \quad \text{--- (1)}$$

$$V_6 = -1 \quad \text{--- (2)}$$

$$V_6 - V_5 = 5 \quad \text{--- (3)}$$

$$V_x = V_2 \quad \text{--- (4)}$$

$$0.5V_x = \frac{V_5 - V_4}{10}$$

Calculate there mesh current  
labeled in cct below

super mesh  $\{I_2, I_1\}$   $\{I_3, I_1\}$

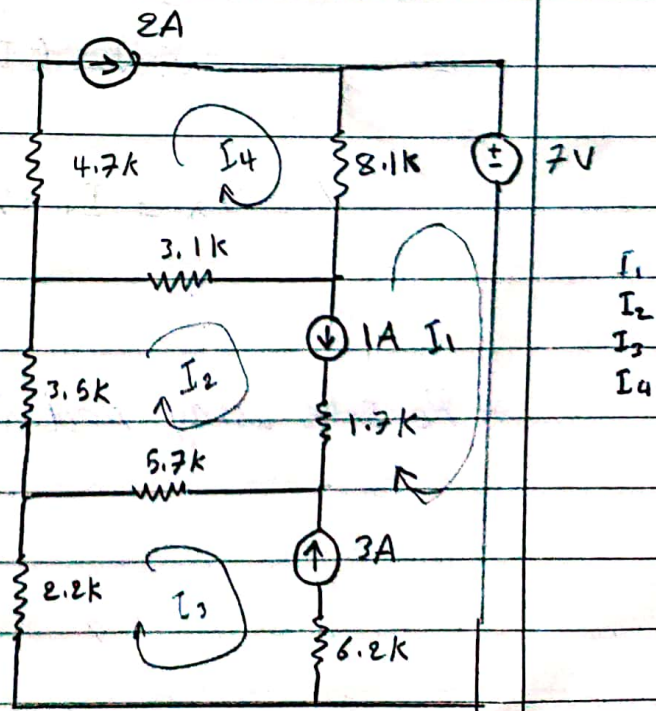
$$I_4 = 2 \quad \text{--- (1)}$$

Kvl at  $I_1, I_2$

$$+7 + 2.2I_3 + 3.5I_2 + 3.1(I_2 - I_4) + (I_1 - I_4)8.1 = 0$$

$$I_2 - I_1 = 1 \quad \text{--- (2)}$$

$$I_1 - I_3 = 3 \quad \text{--- (4)}$$

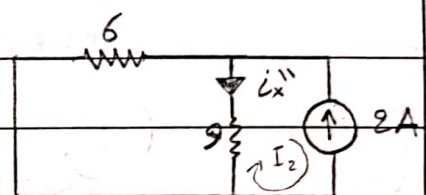
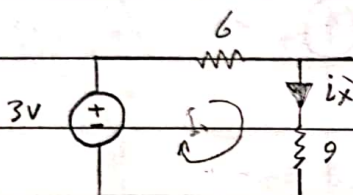
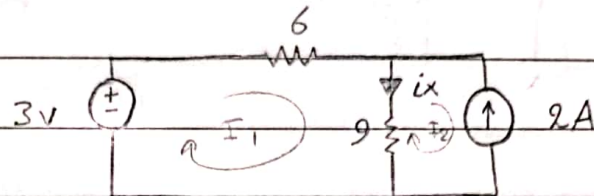


التأثير الكلي للمصادر = تأثير كل مصدر على حده

CH:5

## « Super Position »

\* إذا أردنا اللفاء مصدر الفولتية  
نحنه لشورت <sup>Short</sup> وإذا أردنا اللفاء  
مصدر التيار فنحول <sup>Open Circuit</sup>



$$i_x = i_x' + i_x''$$

حل السؤال بطريقة Super mesh

$$I_2 = -2 \text{ — } \textcircled{1}$$

$$I_1 \Rightarrow -3 + 6I_1 + 9(I_1 - I_2) = 0$$

$$-3 + 6I_1 + 9I_1 + 18 = 0 \Rightarrow 15 + 15I_1 = 0$$

$$\boxed{I_1 = -1 \text{ Amp}}$$

$$i_x = I_1 - I_2 = -1 + 2 \Rightarrow \boxed{i_x = 1 \text{ Amp}}$$

حل السؤال بطريقة Super position

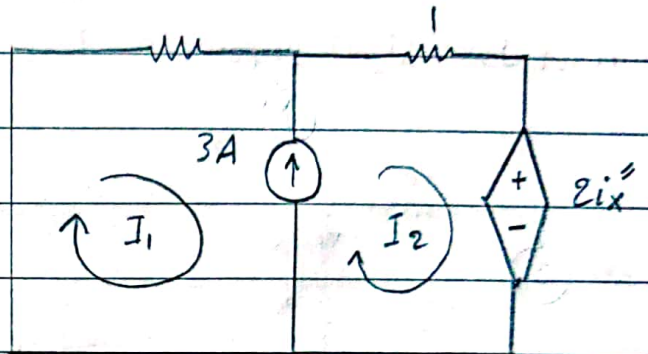
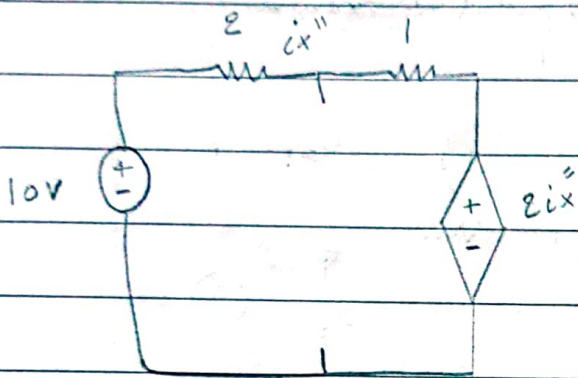
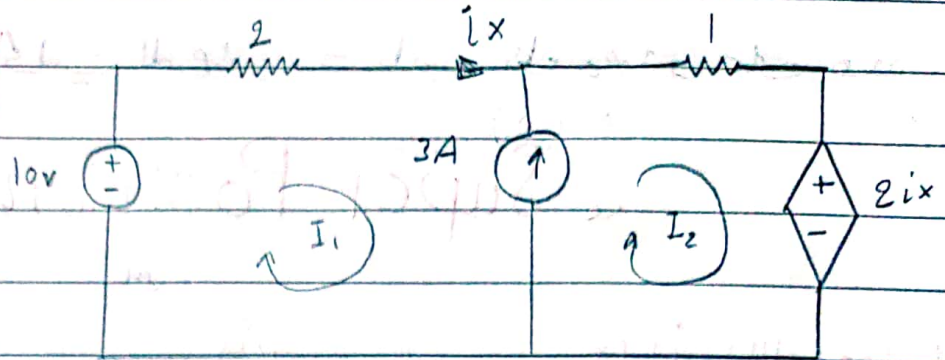
$$i_x' = \frac{3}{15} = 0.2 \text{ A}$$

$$i_x'' = \frac{\text{التيار الكلي} \times \text{المقاومة البقية}}{\text{مجموع المقاومتين}}$$

$$i_x'' = \frac{2 \times 6}{9 + 6} = 0.8$$

$$i_x = 0.2 + 0.8 = 1 \text{ Amp}$$

you can't ignore \*  
Depended  
Source.



Sol KVL  $I_1$

$$2ix + I_2 + 2ix = 0 \quad \text{--- (1)}$$

$$I_2 - ix = 3 \quad \text{--- (2)}$$

$$ix = -0.6A$$

$$-10 + 2ix'' + ix'' + 2ix'' = 0$$

$$ix'' = 2$$

$$= -0.6 + 2 = 1.4$$

KVL  $I_1, I_2$

Super Mesh  $I_1, I_2$  الكس

$$I_2 - I_1 = 3$$

$$-10 + 2I_1 + I_2 + 2I_1 = 0$$

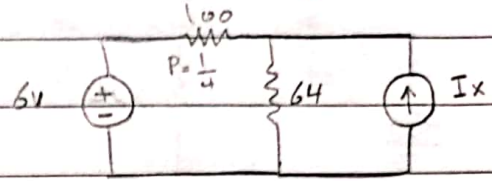
$$I_1 = 1.4$$

$$I_1 = ix$$

Ex: Determine the Maximum Positive Current  $i_x$  Before any resistor exceeds its power rating.

or: Calculated  $i_x$  such that

$$P_{100} = \frac{1}{4} \text{ W}$$



$$P = I^2 R$$

\* في التيار بكل مقاومه قبل ما تطلع  $i_x$

بعدين نفوض  $I_1$  مرة ونطلع منو  $i_x$

وبعدين نفوض  $I_2$  مرة اخرى ونطلع منو  $i_x$

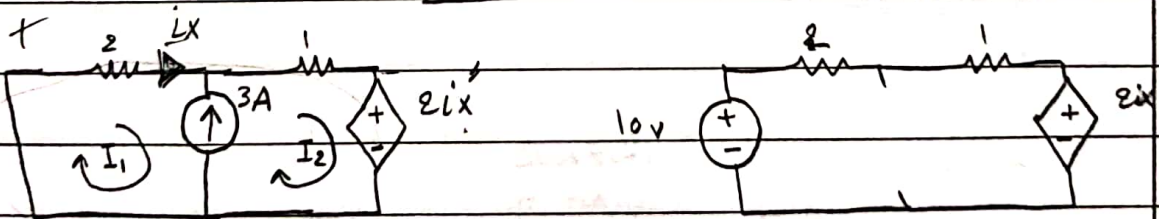
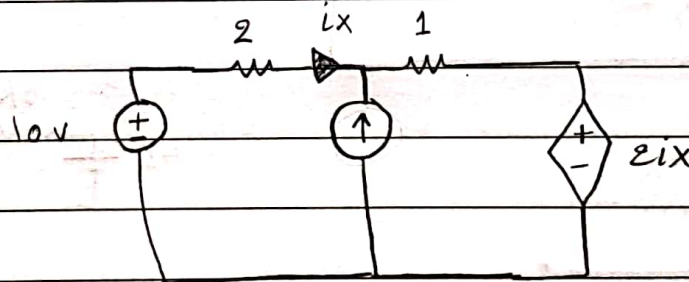
$$\frac{1}{4} = I_1^2 \cdot 100$$

$$I_1 = 50 \text{ mA}$$

$$P_{64} = I_2^2 \cdot 64$$

$$I_2 = 62.5 \text{ mA}$$

إعادة شرح المثال في الصفحة السابقة:



$$I_2 - I_1 = 3 \quad \text{--- (1)}$$

$$-10 + 2i_x' + i_x' + 2i_x' = 0$$

KVL Super Mesh  $I_1, I_2$

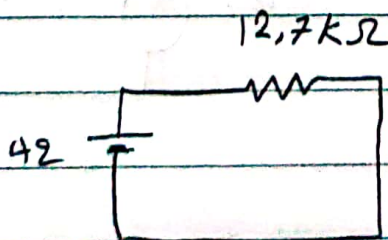
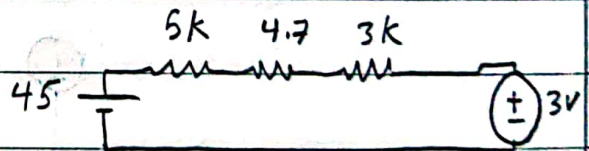
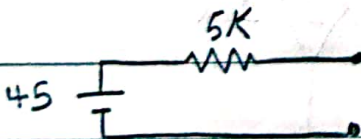
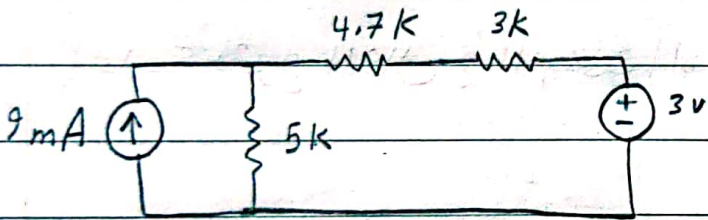
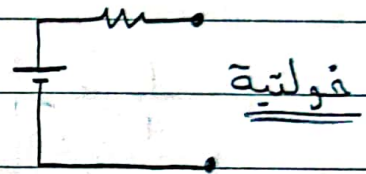
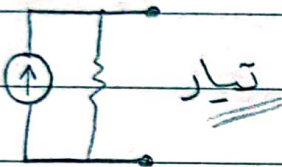
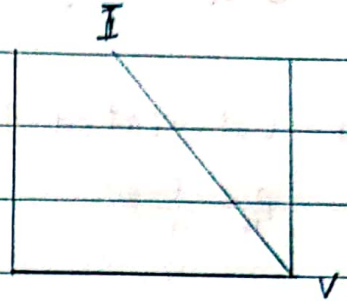
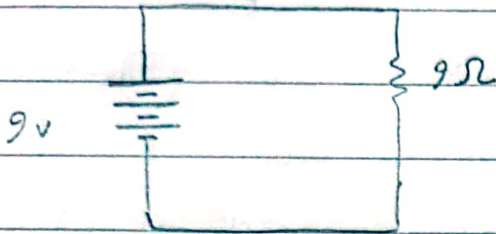
$$i_x' = 2$$

$$2I_x'' + I_2 + 2I_x'' = 0$$

$$i_x'' = -1$$

$$i_x = 2 + (-1) = 1 \text{ Amp}$$

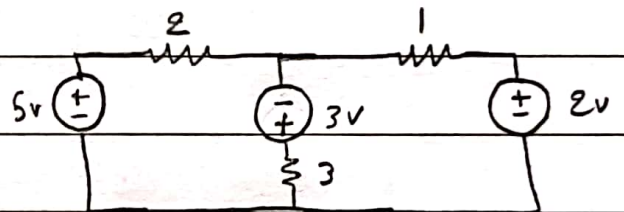
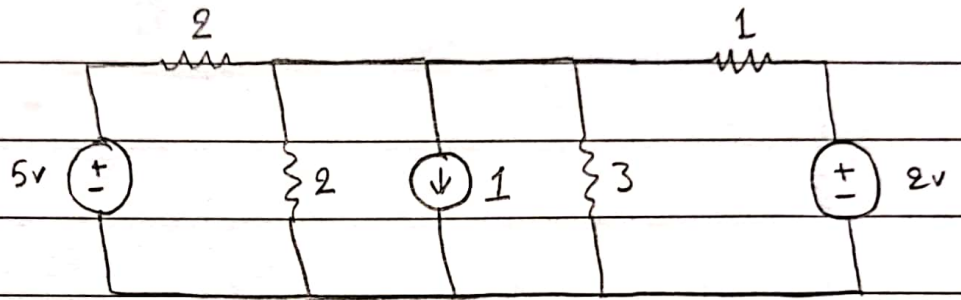
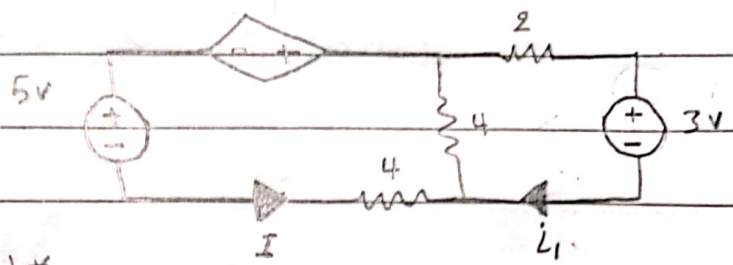
## « Source Transformation »



$$I = \frac{42}{12,7} = 3,2 \text{ mA}$$

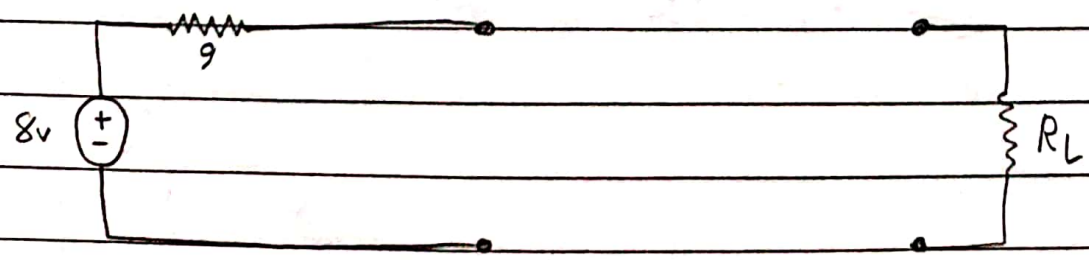
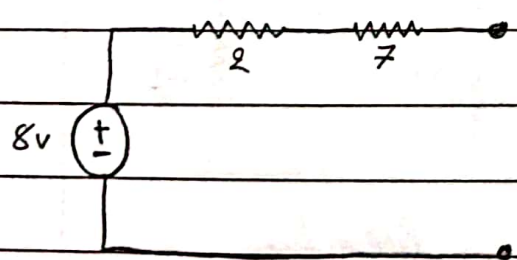
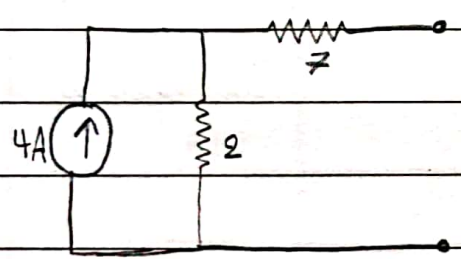
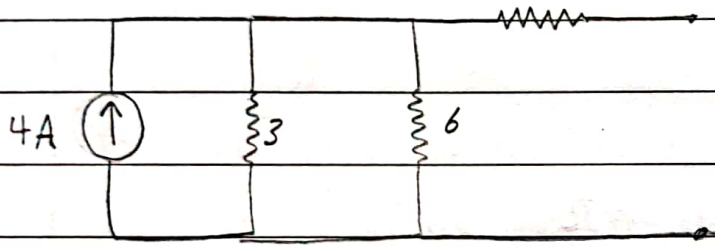
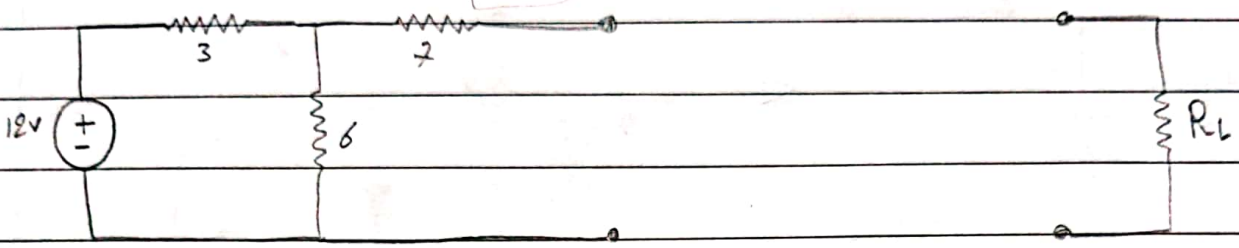
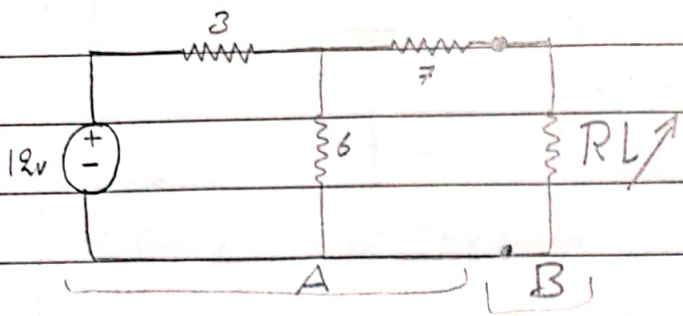
Source بال  
Transformation

\* لا تسول في فرع تحتاجو بعدين



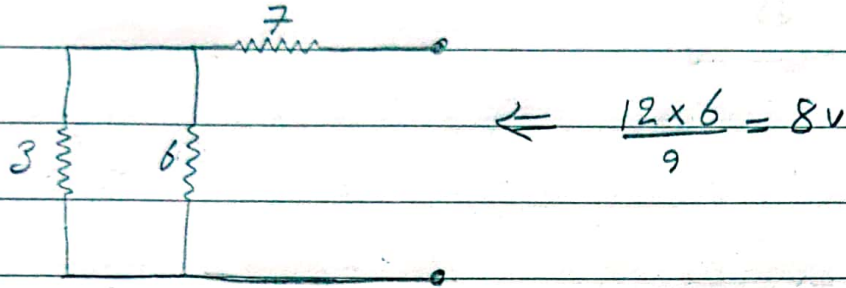
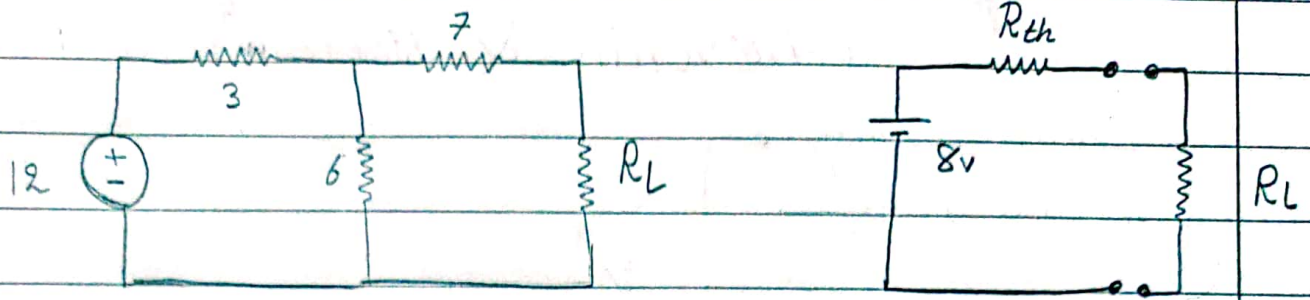


# { Thévenin & Norton }

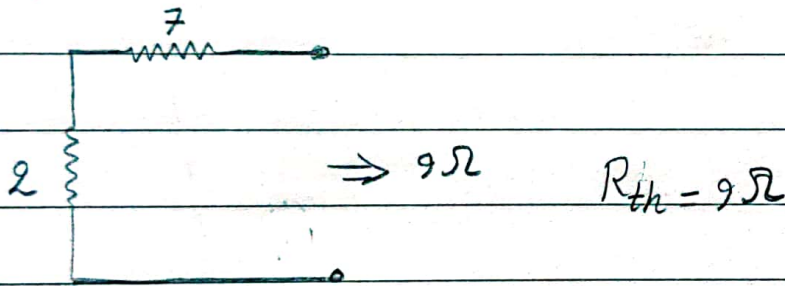


إذ  $R_L$  معلوم تطبيق نطرح التيار

Ex 3

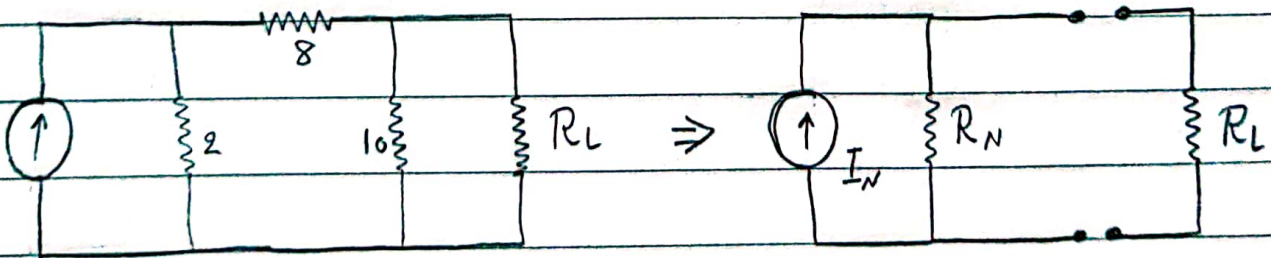


$$\leftarrow \frac{12 \times 6}{9} = 8V$$

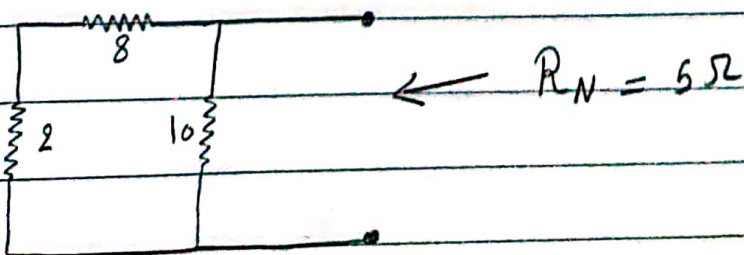


$$\Rightarrow 9\Omega \quad R_{th} = 9\Omega$$

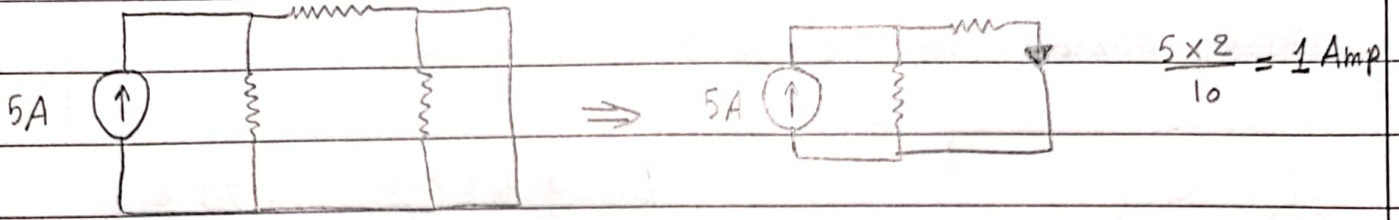
Ex: find Norton Eq, cct



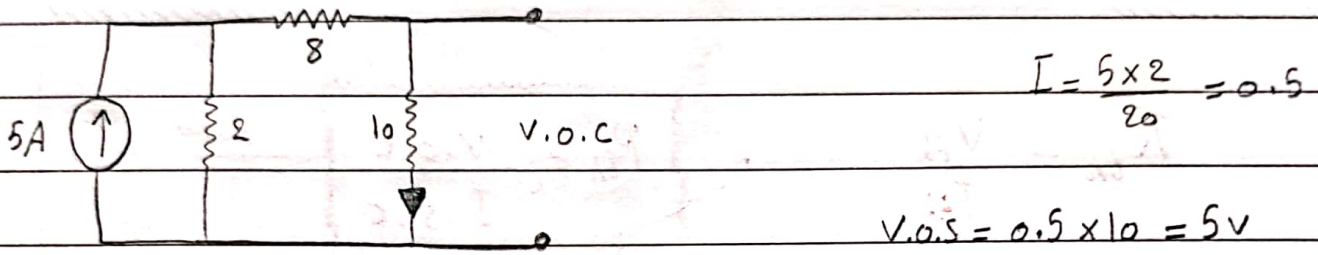
$$R_N = R_{th}$$



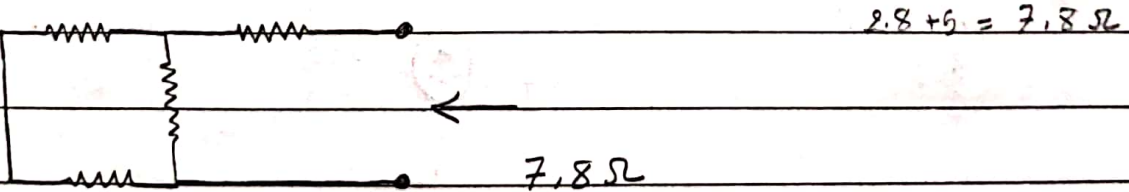
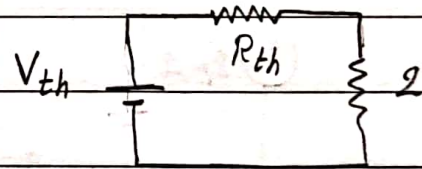
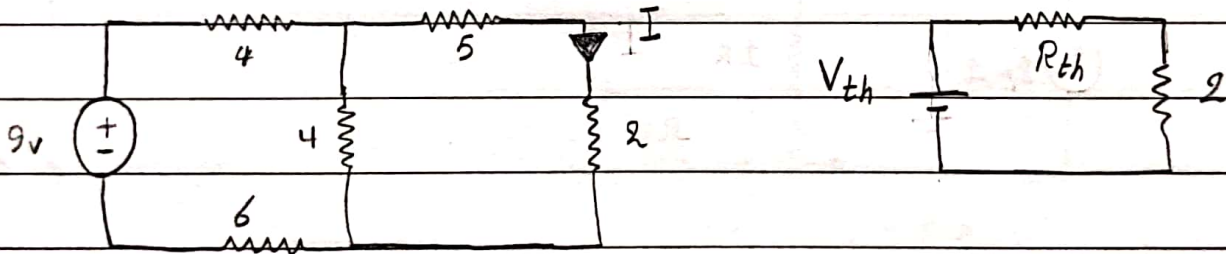
$$\leftarrow R_N = 5\Omega$$



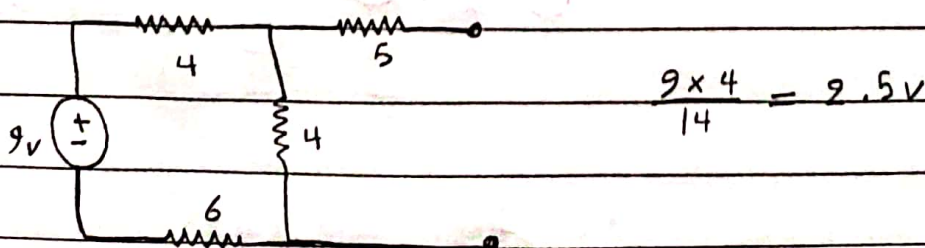
Resolve using Thévenin



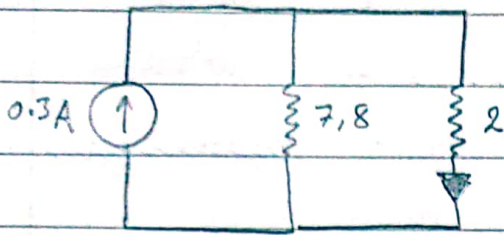
Find the current through the 2 ohm resistor using Thévenin



$V_{th} = V_{O.C.}$



Find Norton Eq.

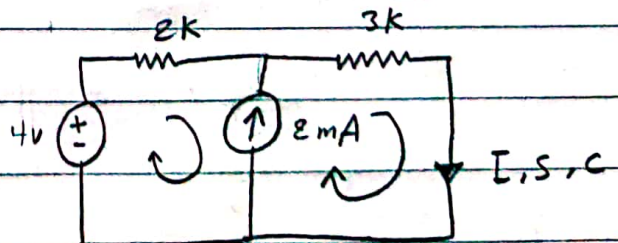
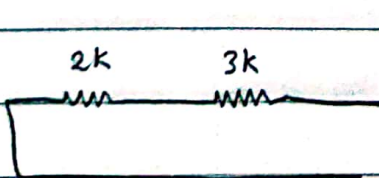
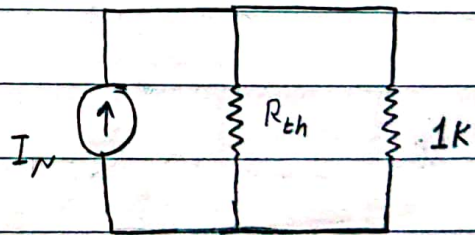
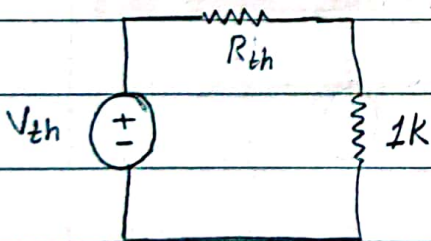
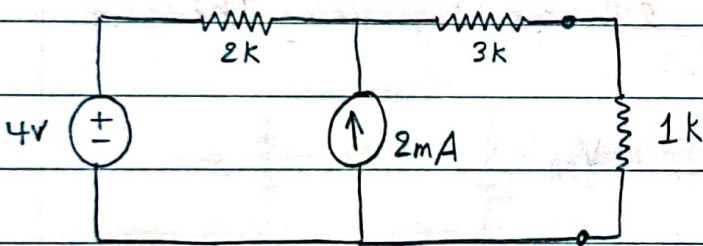


$$I = \frac{0.3 \times 7.8}{9.8} = 0.23 \text{ A}$$

$$R_{th} = \frac{V_{th}}{I_{th}}$$

$$R_{th} = \frac{V_{o.c}}{I_{s.c}}$$

Ex find Norton Eq at 1kΩ



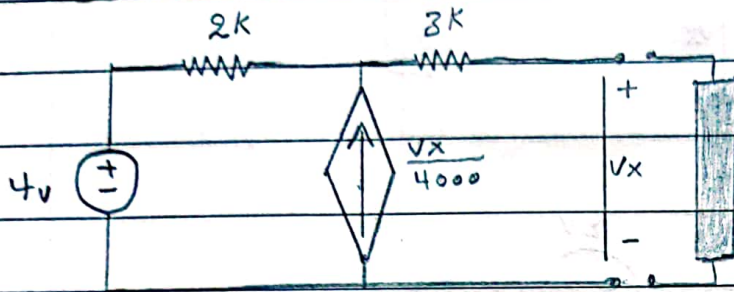
$$-V_{o.s} + 4 + 4 = 0$$

$$V_{o.c} = 8$$

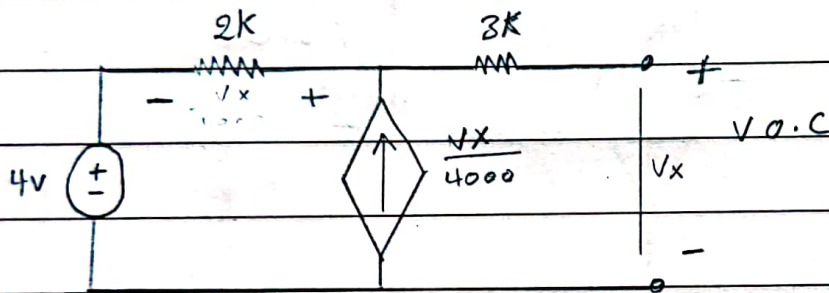
$$I_{s.c} = 1.6 \text{ mA}$$

\* في كل دائرة مستقلة، لا بد من  
 V.O.S و I.S.C

الملاحظة:  $R_{th} = R_N$   
 $V_{th} = I_N \cdot R_N$   
 $R_{th} = \frac{V_{th}}{I_{th}}$



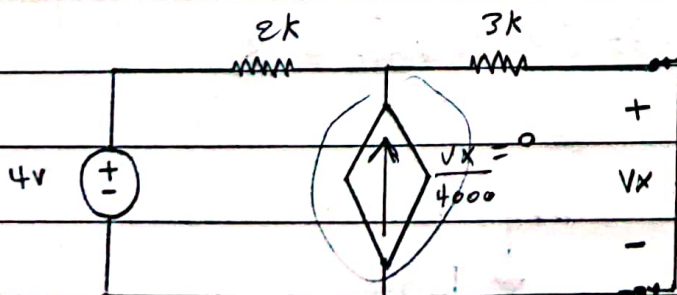
Find Thevenin in circuit



$$KVL = -V_x + 0 + \frac{2 \times 10^3 V_x}{4000} + 4 = 0$$

$$V_x = V_{O.C}$$

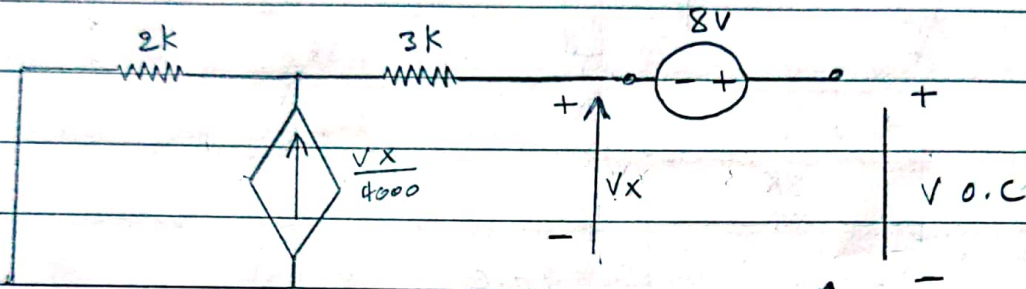
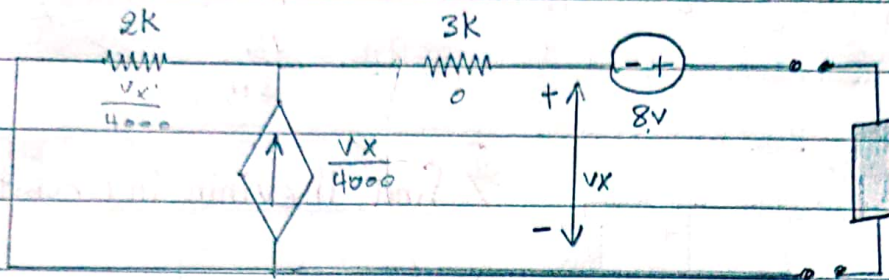
$$V_{O.C} = 8V$$



$$I_{S.C} = \frac{4}{(2+3)k} = \frac{4}{5} = 0.8 \text{ mA}$$

$$R_{th} = \frac{8}{0.8} = 10 \text{ k}\Omega$$

Find thevenin Eq. circuit for the circuit below

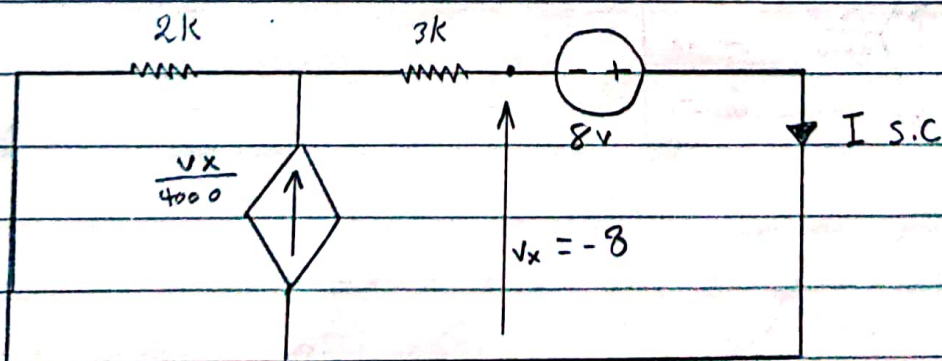


$$-V_{o.c} + 8 + 0 + \frac{2 \times 10^3 V_x}{4000} = 0 \quad \text{--- (1)}$$

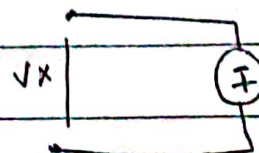
$$-V_{o.c} + 8 + V_x = 0 \quad \text{--- (2)}$$

$$V_{o.c} = 8 + V_x$$

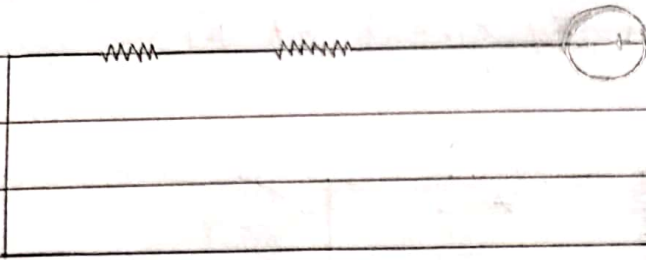
$$\therefore V_{o.c} = 8$$



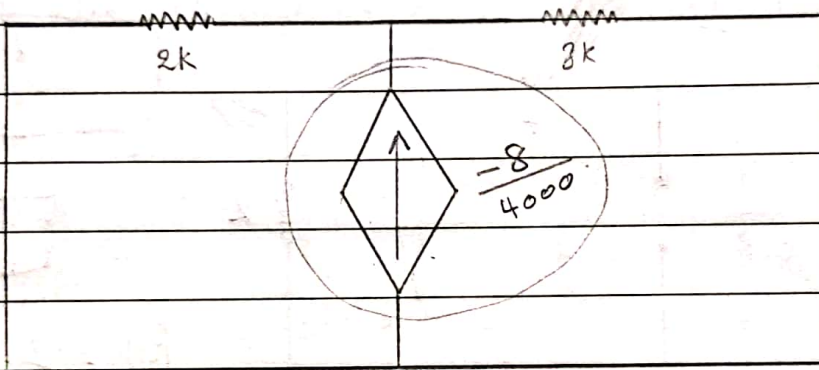
$$V_x = -8$$



Apply Super Position

 $I_{sc}$ 

$$I_{s.c} = \frac{8}{5} = 1.6 \text{ mA}$$

 $I_{sc}$ 

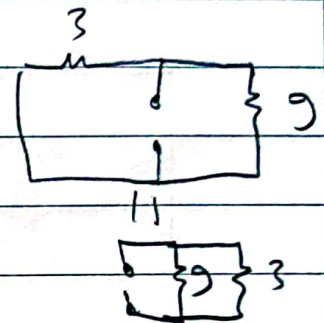
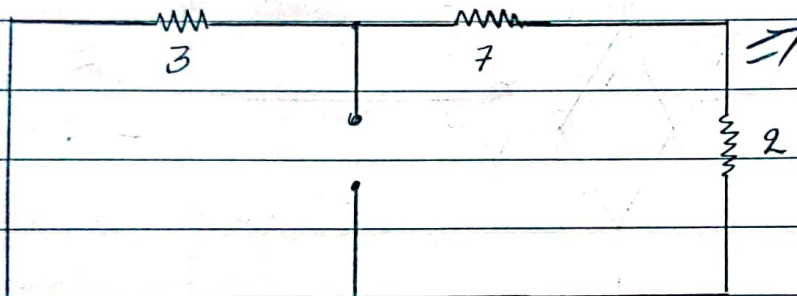
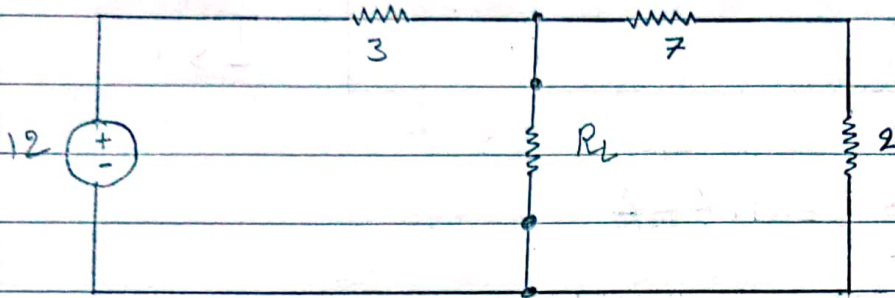
$$\frac{-8}{4000} * \frac{2k}{5k} = -0.8 \text{ mA}$$

$$I_{s.c} = 1.6 - 0.8 = 0.8 \text{ mA}$$

$$I_{s.c} + I_{s.c}$$

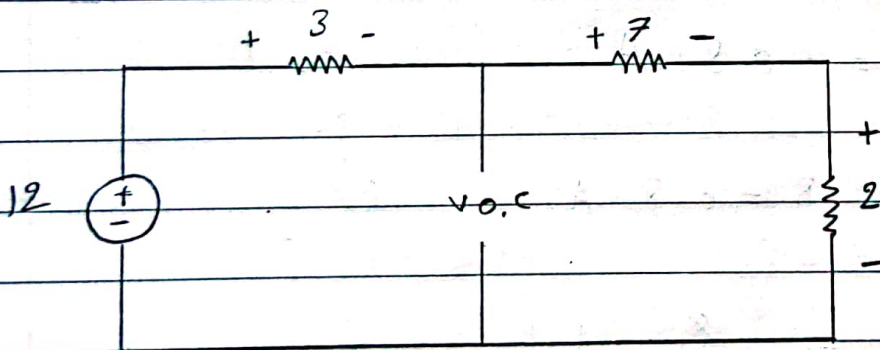
$$R_{th} = \frac{V_{o.c}}{I_{s.c}} \Rightarrow \frac{8}{0.8} = 10k$$

Find the Thévenin Eq circuit at  $R_L$



$$\frac{3 \times 7}{12} = 1.75$$

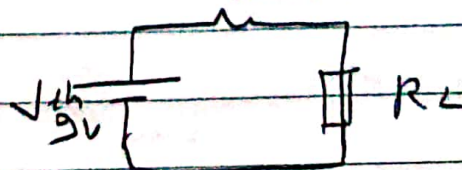
$$R_{Th} = 2.25 \Omega$$



$$V_{o.c} = \frac{12 \times 2}{12} = 2V$$

$$I = \frac{12}{3+7+2} = 1mA$$

$$V_{o.c} = 9V$$

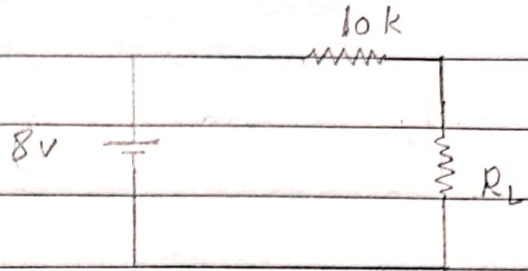




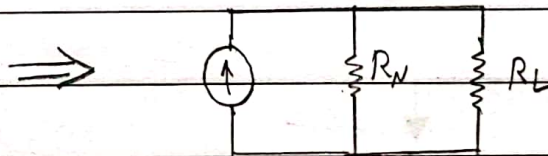
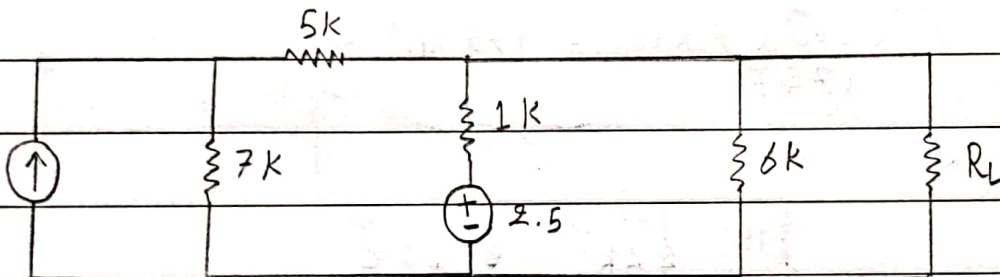
find the power diss by  $R_{th} = 1K$

$$P = I^2 R$$

$$I = \frac{8}{11} = 0.72$$



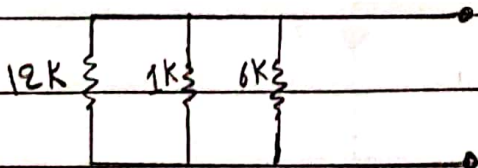
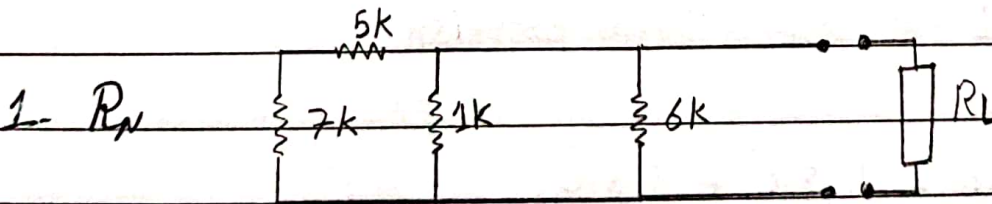
use Norton theory to reduce the following circuit



الطلب

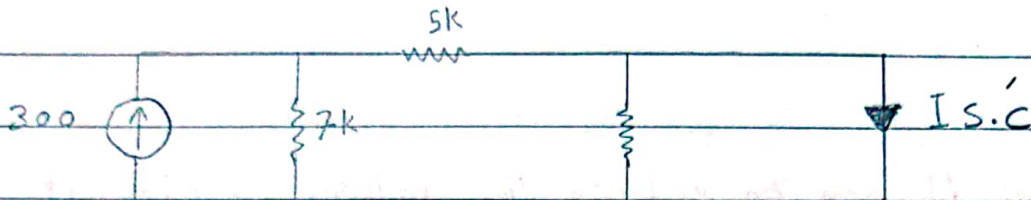
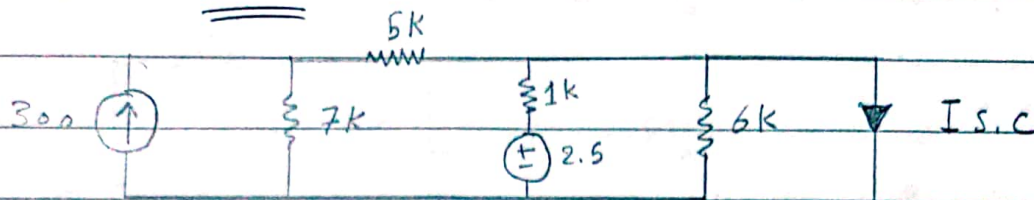
الحل

$$R_{th} = R_N \quad , \quad I_N = I_{S.C}$$



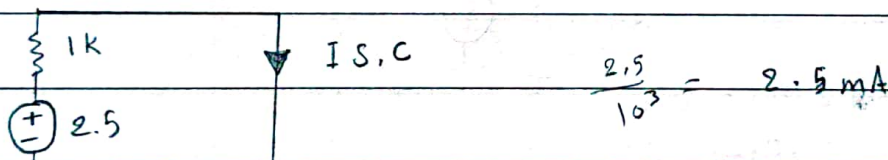
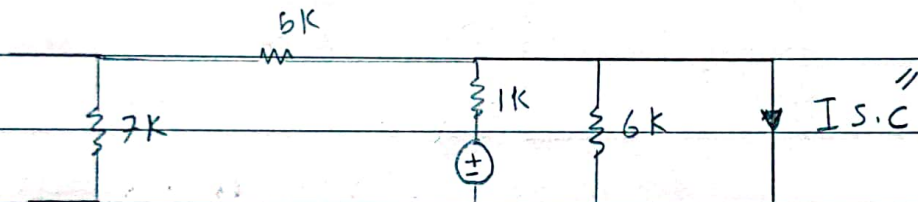
$$R_{th} = 0.8 \text{ k}\Omega$$

$$I_N = \underline{\underline{I_{s.c}}}$$



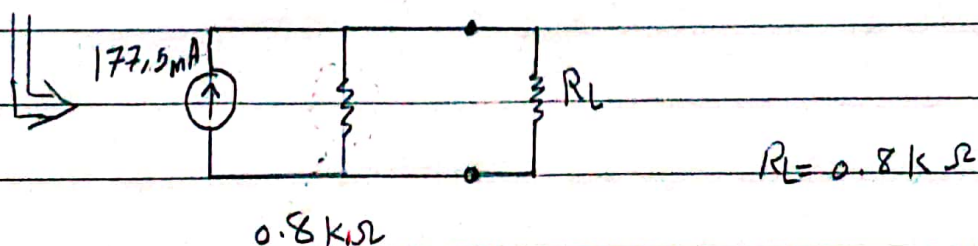
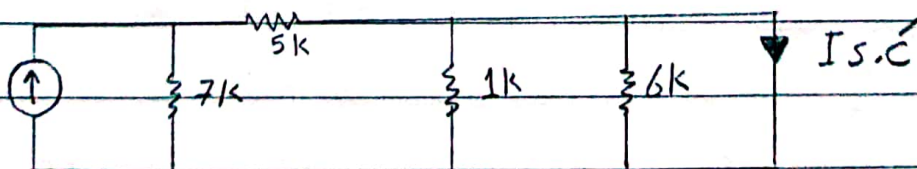
$$I_{s.c'} = \frac{10^{-3} \times 300 \times 7 \times 10^3}{7 + 5} = 175 \text{ mA}$$

↑  
البعد

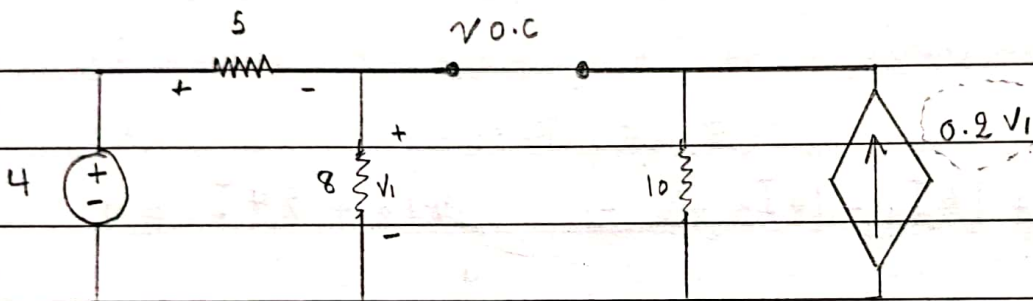
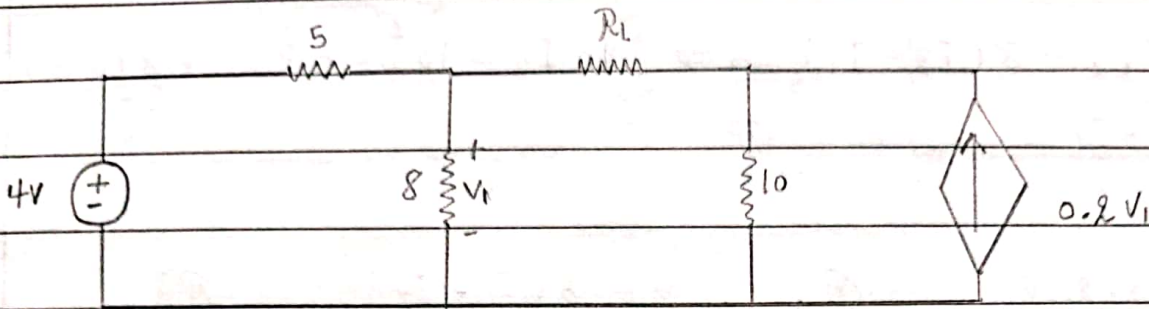


To find  $I_{s.c}$  use Super position

$$I_{s.c} = I_{s.c'} + I_{s.c''}$$



Find the value of the  $R_L$  in sure maximum absorbed Power  $R_L$   $R_L$  آوجد أقيم نقل للقدره في  $R_L$



$$v_1 = \frac{4 \times 8}{13} = 2.46 \text{ V}$$

$$0.2 \times (2.46) = 0.49 \text{ A}$$

$$V_{10} = 10 \times 0.49 = 4.9 \text{ V}$$

KVL  $V_{o.c}$

$$-2.46 + V_{o.c} + 4.9 = 0$$

$$V_{o.c} = -2.44$$

$$-4 + 5I_1 + 8(I_1 - I_2) = 0 \Rightarrow 4 + 5I_1 + 8I_1 - 8I_2 = 0$$

$$\Rightarrow \boxed{-4 + 13I_1 - 8I_2 = 0} \quad \text{--- (1)} \quad *4$$

$$10(I_2 - I_3) - 8(I_2 - I_1) = 0 \Rightarrow 10I_2 - 10I_3 - 8I_2 + 8I_1 = 0$$

$$\Rightarrow \boxed{2I_2 + 8I_1 - 10I_3 = 0} \quad \text{--- (2)}$$

$$I_3 = -0.2 V_1 \quad \text{--- (3)} \quad V = 8(I_1 - I_2) \quad \text{--- (4)}$$

$$I_3 = -1.6I_1 + 1.6I_2$$

$$2I_2 + 8I_1 + 16I_1 - 16I_2 = 0 \Rightarrow -14I_2 + 24I_1 = 0 \quad \text{--- (5)} \quad *2$$

$$-56I_2 + 96I_1 = 0$$

$$-28 + 91I_1 - 56I_2 = 0 \quad \text{--- (6)}$$

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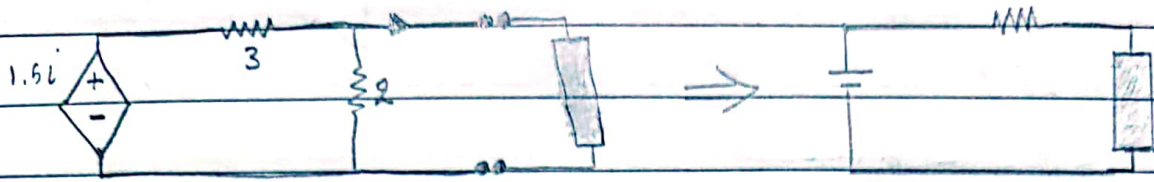

$$-28 + 5I_1 = 0 \quad I_1 = \frac{28}{5} = 5.6$$

$$-14I_2 - 134.4 = 0 \quad I_2 = -9.6$$

$$R_{th} = \frac{-2.44}{-9.6} = 0.25 \Omega$$

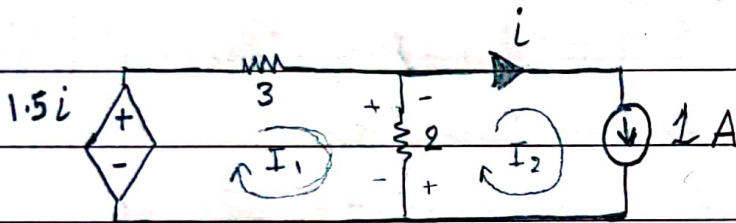
أوجد مكافئ ثفنن للدائرة أدناه

find the Thévenin eq circuit below



$$R_{th} = \frac{V_{o.c}}{I_{s.c}} = \frac{V_{o.c}}{0} = \infty$$

\* نلاحظ أن الدائرة تحتوي على مصدر يعتمد فقط في حاله أنشيف مصدر تيار أو مصدر فولتية بقيمة افتراضية 1 مثلا ويكون المطوق مكان ال  $R_L$ .



$$R_{th} = \frac{V}{I}, \quad I_2 = 1$$

KVL at  $I_1$

$$-1.5i + 3I_1 + 2(I_1 - I_2) = 0$$

$$-1.5i + 3I_1 + 2I_1 - 2I_2 = 0$$

$$-1.5i + 5I_1 - 2I_2 = 0 \quad \dots \textcircled{1}$$

$$I_2 = -1 = i$$

$$-1.5 + 5I_1 - 2 = 0$$

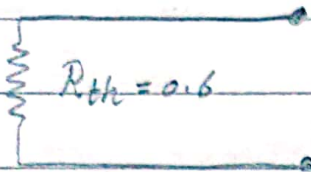
$$V = 2(0.3)$$

$$5I_1 = 3.5$$

$$I_1 = 0.7$$

$$V_2 = 0.6 \text{ v}$$

$$R_{th} = \frac{V_{test}}{I_{test}} = \frac{0.6}{1} = 0.6 \Omega$$



وجود مصدر متناوب

عدم وجود مصدر متناوب

$$R_{th} = \frac{V_{o.c}}{I_{s.c}}$$

or

نضيف  $V_T$  أو  $I_T$ 

$$R_{th} = R_{eq}$$

$$V_{th} = V_{o.c}$$

$$R_N = R_{eq} = R_{th}$$

$$I_N = I_{s.c}$$

Thévenin

Norton